

$|S\rangle \equiv$  unstable state

$$a(t) = \langle S | e^{-iHt} | S \rangle$$

$$P(t) = |a(t)|^2$$

$$P(t) \approx 1 - \frac{t^2}{T_2^2} + \dots$$

always non-exp for short times!!!

- two-level case
- $n$ -level case and  $n \rightarrow \infty$  (when  $|S\rangle$  is genuinely non unstable state)
- "real" Rabi was in an ex.

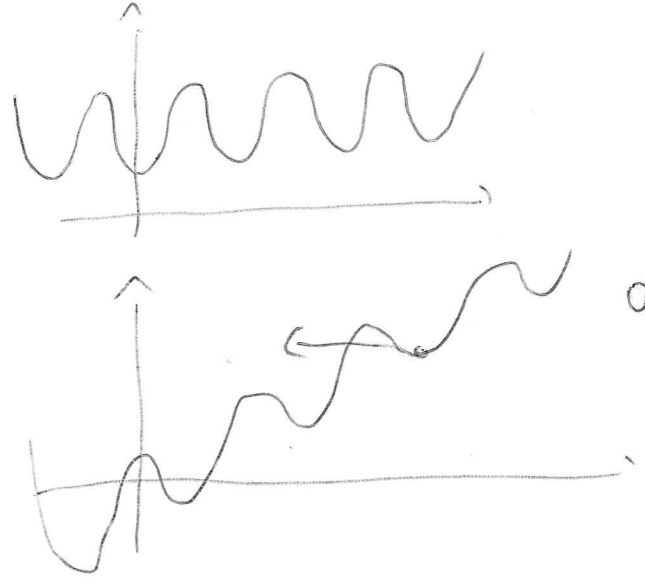
Haro et al (WineLand)

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$$P(t) = \cos^2$$



Raijen et al



for a large enough!!!

• free Hamiltonian

$$H = M_0 |S\rangle \langle S| + \sum_{\mathbf{k}} \omega_{\mathbf{k}} |\mathbf{k}\rangle \langle \mathbf{k}| + \sum_{\mathbf{k}} g \frac{f(\mathbf{k})}{\sqrt{L}} (|S\rangle \langle \mathbf{k} + \mathbf{k}\rangle + \text{h.c.})$$

• Ericksen argument

$$\left\{ \begin{array}{l} \sum_{\mathbf{k}} \mapsto L \int_{-\infty}^{\infty} \frac{d\mathbf{k}}{2\pi} \\ |\mathbf{k}\rangle \mapsto \frac{1}{\sqrt{L}} |\mathbf{k}\rangle \end{array} \right.$$

• NR-BW limit

Non-relativistic  
propagator

spectral function

Model of Thomas

Other interesting experiments:

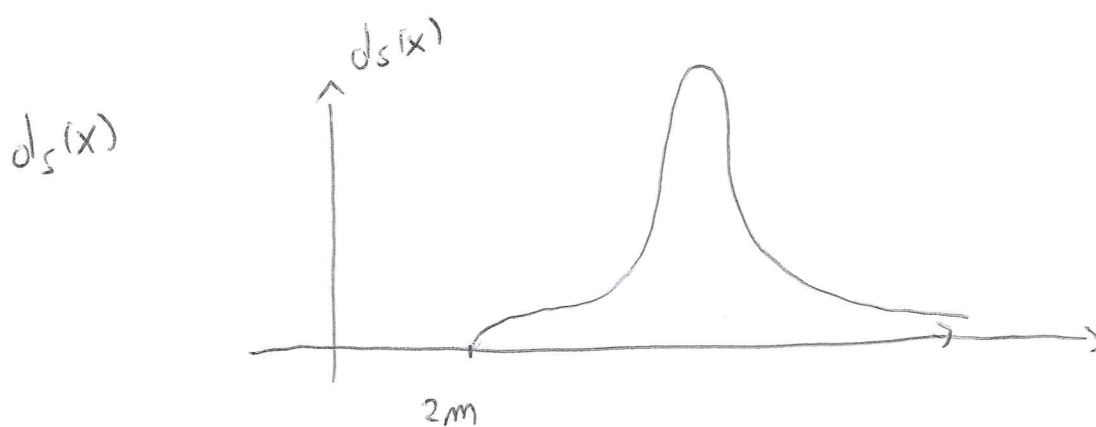
• Ketterle et al

• Horobe et al

We then turned to QFT

$$\mathcal{L}_{\text{int}} = g S \varphi^2$$

$$\Gamma_{S \rightarrow \varphi\varphi} = \frac{|\vec{k}|}{8\pi M_S^2}$$



$$\int_0^{\infty} ds(x) dx = 1$$

$$a(t) = \int_0^{\infty} e^{-ixt} ds(x) dx$$

$$P(t) = |a(t)|^2 = 1 - t^2/\gamma^2 + \dots \quad \text{also in QFT}$$

Not only scalar fields...

$$\mathcal{L} = g_H \bar{\Psi} \Psi$$



$$\mathcal{L} = e_u \bar{\psi}^u \psi \quad \text{e meson}$$

Not only two-body decay

$$P \rightarrow \phi_1 \phi_2 \phi_3$$

"directly" or with an



Delta plot

(non-Fund, but  
effective, see in decay)

Last thing:  $\sigma, \pi \rightarrow$  chiral symmetry, its spont. and expl. breaking  
and the decay  $\sigma \rightarrow \pi\pi$  in a simplified model!

$f_0(500)$

Determination of its properties.

Coupling to pions

$\pi\pi \mapsto f_0(500) \mapsto \pi\pi$

Achtung: resonances are not always "bumps" in the cross section.

$f_0(980)$ , for instance, appears as a "dip".

Reason:

$$\sigma \propto \left| \frac{\mathcal{M}_{f_0(980) \rightarrow \pi\pi}}{(s - M_{f_0(980)}^2 + i\Gamma_{f_0(980)} M_{f_0(980)})} - \frac{\mathcal{M}_{\sigma \rightarrow \pi\pi}}{(s - M_{\sigma}^2 + i\Gamma_{\sigma} M_{\sigma})} \right|^2$$

KLOE2 decays

$$\eta \rightarrow \pi\pi\pi$$

$(m_d - m_u)$

$$\eta \rightarrow \pi^+\pi^-\pi^0$$

$$\eta \rightarrow \pi^0\pi^0\pi^0$$

low-energy decays. Important for precision tests of chpt.  
(still, there are some problems here).

Determination of  $m_u$  and  $m_d$ .

$$\eta \rightarrow \pi^+\pi^-\gamma$$

(New result ... lower than previous event.



other channels:

$$\phi \rightarrow \eta e^+e^- ; \eta \rightarrow \gamma\gamma, \pi^0 \rightarrow \gamma\gamma, \eta' \rightarrow \gamma\gamma$$

exercise :

Which is the coupling of  $\eta$  and  $\pi^0$  to  $\gamma\gamma$ ?

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How can we write it? Which is the ratio?

$$\pi^0 = \frac{1}{\sqrt{2}} (\bar{u}u - \bar{d}d)$$

$$\eta_N = \frac{1}{\sqrt{2}} (\bar{u}u + \bar{d}d)$$

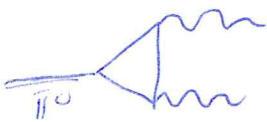
$$\eta_S = \bar{s}s$$

$$\mathcal{L} = \alpha_{\pi^0} \pi^0 F_{\mu\nu} \tilde{F}^{\mu\nu} + \alpha_{\eta_N} \eta_N F_{\mu\nu} \tilde{F}^{\mu\nu} + \alpha_{\eta_S} \eta_S F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$\Gamma_{\pi^0 \rightarrow \gamma\gamma} = \frac{\alpha_{\pi^0}^2}{4\pi} M_{\pi^0}^2$$

Can we evaluate the ratio  $\alpha_{\pi^0} / \alpha_{\eta_N}$ ?

Actually Yes!!! For that we need to look at the microscopic treatment.



$$\alpha_{\pi^0} \propto \sqrt{\frac{1}{2}} \left( \frac{4}{9} - \frac{1}{9} \right)$$

$$\alpha_{\eta_N} \propto \sqrt{\frac{1}{2}} \left( \frac{4}{9} + \frac{1}{9} \right)$$

$$\alpha_{\eta_S} \propto \frac{1}{9}$$

$$\frac{\Gamma_{\eta_N \rightarrow \gamma\gamma}}{\Gamma_{\pi^0 \rightarrow \gamma\gamma}} = \frac{M_{\eta_N}^3}{M_{\pi^0}^3} \cdot \frac{\left[ \sqrt{\frac{1}{2}} \cdot \frac{5}{9} \right]^2}{\left[ \sqrt{\frac{1}{2}} \cdot \frac{5}{9} \right]^2}$$

$$= \frac{M_{\eta_N}^2}{M_{\pi^0}^2} \cdot \frac{9}{25}$$

But indeed there is also mixing!

$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos \alpha_P & + \sin \alpha_P \\ -\sin \alpha_P & \cos \alpha_P \end{pmatrix} \begin{pmatrix} \eta_N \\ \eta_S \end{pmatrix}$$

$$\begin{pmatrix} \eta_N \\ \eta_S \end{pmatrix} = \begin{pmatrix} \cos \alpha_P & -\sin \alpha_P \\ \sin \alpha_P & \cos \alpha_P \end{pmatrix} \begin{pmatrix} \eta \\ \eta' \end{pmatrix}$$

ergo:

$$\mathcal{L} = \alpha_{\eta^0} \eta^0 \tilde{F} \tilde{F} + \alpha_{\eta_N} (c \eta - s \eta') \tilde{F} \tilde{F} + \alpha_{\eta_S} (s \eta + c \eta')$$

$$= \alpha_{\eta^0} \eta^0 \tilde{F} \tilde{F} + (\alpha_{\eta_N} c + \alpha_{\eta_S} s) \eta \tilde{F} \tilde{F}$$

$$+ (-\alpha_{\eta_N} s + \alpha_{\eta_S} c) \eta' \tilde{F} \tilde{F}$$

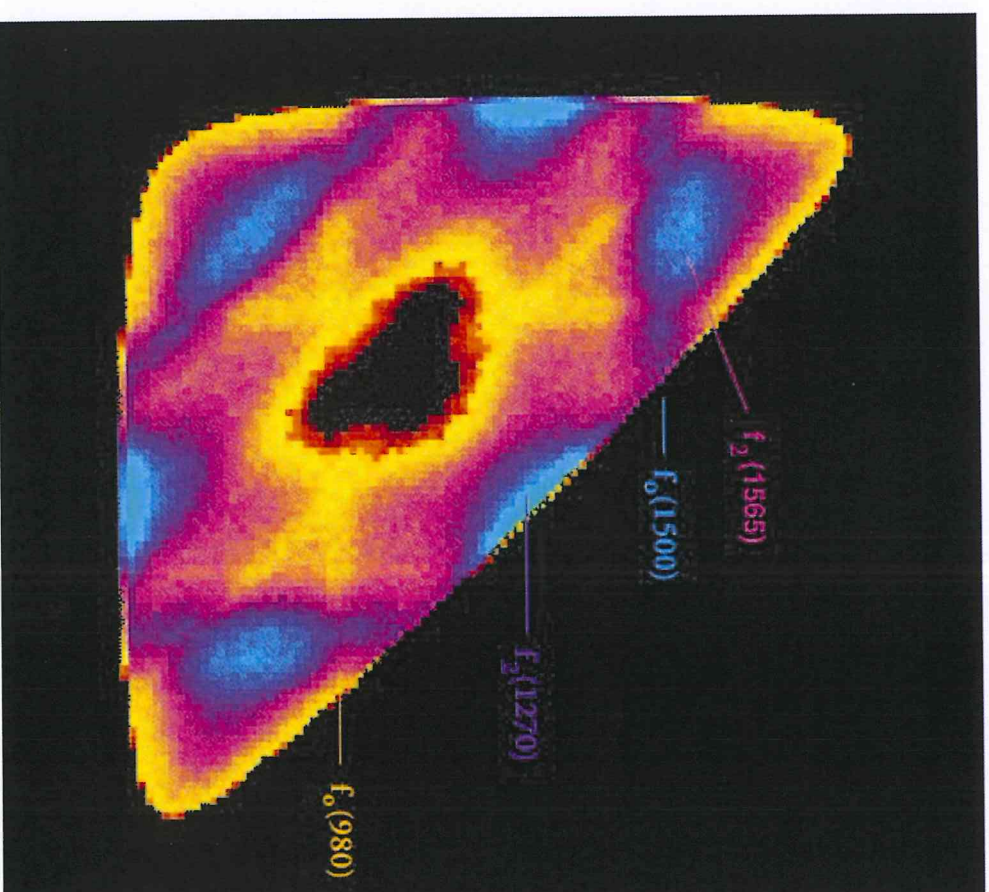
$$\frac{\int_{\eta^0 \rightarrow \delta\delta} \int_{\eta_N \rightarrow \delta\delta} \int_{\eta_S \rightarrow \delta\delta} M_{\eta^0}^3}{\int_{\eta^0 \rightarrow \delta\delta} M_{\eta^0}^3} = \frac{M_{\eta^0}^3 (\alpha_{\eta_N} c + \alpha_{\eta_S} s)^2}{\alpha_{\eta^0}^2} = \frac{M_{\eta^0}^2 \left( \sqrt{\frac{1}{2}} \cdot \frac{5}{9} c + \frac{1}{9} s \right)^2}{\left( \sqrt{\frac{1}{2}} \cdot \frac{3}{9} \right)^2}$$

$$\alpha_P \approx -36^\circ$$



# Crystal Barrel

$\bar{p}p \rightarrow \pi^0\pi^0\pi^0$  Dalitz plot



700000 events =  $6 \times 700000$  entries

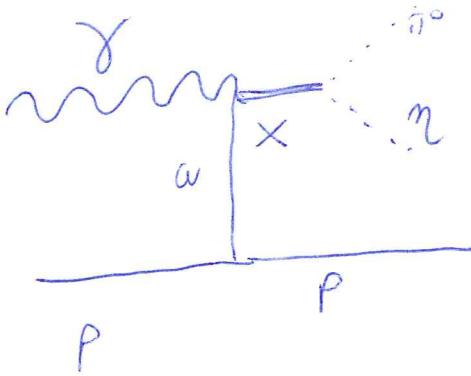
N.B: The physics of  $\eta, \eta'$  mesons studied at WASA@COSY!  
(Jülich).

4'

J lab  
(GlueX, CLAS)

$\gamma + p \rightarrow \text{example!}$

$\gamma p$



one can "factorize" this process in

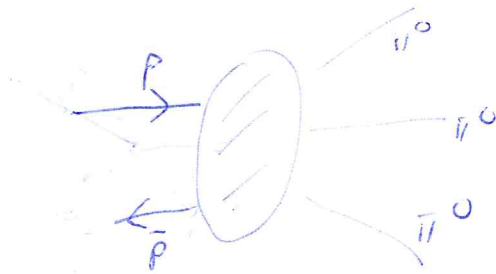
$\sigma_{\text{tot}} =$  "production", "decay"



$\Gamma_{X \rightarrow \pi^0 N}$

$$\bar{P}P \mapsto \pi^0 \pi^0 \pi^0$$

Dalitz plot always a crucial tool (3 body in the final state).



Microscopic scheme for the "glueball production" in a gluon rich environment.

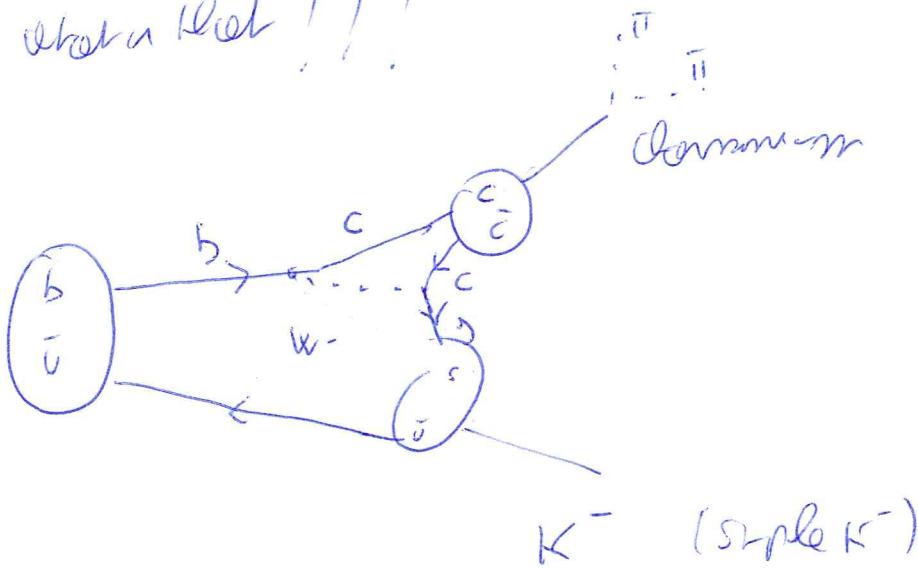
Future panda physics!!!

Exotic and charmless  $B$  decays

Babar

$B \rightarrow K \pi \pi$

X (3872) has been seen...  
what's that???



$W^-$  is flavor changing

◦ LHC b and the  $B_{s0}$  decays

◦ [The last two DPG - Journals ... ]  
L

◦ E(38) state