Parton Momentum Distribution Prior to Equilibrium

Stanisław Mrówczyński

Świętokrzyska Academy, Kielce, Poland & Institute for Nuclear Studies, Warsaw, Poland

in collaboration with Weronika Jas

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Evolution of Parton Momentum Distribution



Elliptic Flow & Equilibration

Success of hydrodynamic models in describing elliptic flow



Equilibration Time

$$\mathbf{v}_{2} \sim \varepsilon = \frac{\langle y^{2} \rangle - \langle x^{2} \rangle}{\langle y^{2} \rangle + \langle x^{2} \rangle}$$

Eccentricity decays due to the free streaming!



U. Heinz, AIP Conf. Proc.739, 163 (2004)

Decay of Eccentricity

free-streaming model

$$f(\mathbf{p},\mathbf{r},t) \sim \exp\left[-\frac{(x-v_x t)^2}{2\sigma_x^2} - \frac{(y-v_y t)^2}{2\sigma_y^2} - \frac{(z-v_z t)^2}{2\sigma_z^2} - \frac{Y^2}{2\Delta Y^2}\right] \frac{P(p_T)}{p_T^2 \operatorname{ch} Y}$$

W. Jas and St. Mrówczyński, arXiv:0706.2273 [nucl-th].

Decay of Eccentricity cont.





Decay of Eccentricity cont.



Momentum Distribution in a Box



$$\int_{-L_z/2}^{L_z/2} dz = \int_{-\infty}^{+\infty} dz \ O_z(z), \quad \int_{-L_z/2}^{L_z/2} dz \ z^2 = \int_{-\infty}^{+\infty} dz \ z^2 O_z(z)$$

$$O(\mathbf{r}) = O_x(x)O_y(y)O_z(z) = \left(\frac{6}{\pi}\right)^{3/2} \exp\left[-\frac{6x^2}{L_x^2} - \frac{6y^2}{L_y^2} - \frac{6z^2}{L_z^2}\right]$$

Evolution of Momentum Distribution



$$\left\langle p_i^2 \right\rangle = \frac{1}{N} \int d^3 r \, O(\mathbf{r}) \int \frac{d^3 p}{(2\pi)^3} p_i^2 f(\mathbf{p}, \mathbf{r}, t), \quad i = L, T$$
$$N = \int d^3 r \, O(\mathbf{r}) \int \frac{d^3 p}{(2\pi)^3} f(\mathbf{p}, \mathbf{r}, t)$$

Evolution of Momentum Distribution cont.

$$\sigma_{x} = \sigma_{y} = L_{x} = L_{y} = 3 \text{ fm}, \quad \sigma_{z} = L_{z} = 1 \text{ fm}$$
Au-Au collision
$$L_{z} = 1 \text{ fm}$$

$$\int_{0}^{0} \frac{\rho(t) = 2 < p_{L}^{2} > / < p_{T}^{2} > 0}{0 + 1 + 1 + 1 + 1 + 2 + 2 + 5} = 0$$

$$\int_{0}^{0} \frac{\Delta Y = 2.5}{\Delta Y = 2.0} = \frac{\Delta Y^{2}}{10^{2}} = \frac{1}{t_{eq}} = \frac{1}{$$

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Evolution of Momentum Distribution cont.

$$\sigma_x = \sigma_y = L_x = L_y = 3 \text{ fm}, \quad \sigma_z = 1 \text{ fm}, \quad L_z = 3 \text{ fm},$$

10⁷ Au-Au collision



Effect of finite formation time

$$f(\mathbf{p},\mathbf{r},t) \rightarrow \Theta(t\sqrt{1-v_z^2}-\tau) f(\mathbf{p},\mathbf{r},t)$$



$$t\sqrt{1-v_z^2}$$
 - parton's proper time

$$-Y_{\max} < Y < Y_{\max}$$

$$\operatorname{th} Y_{\max} = \frac{1}{t} \sqrt{t^2 - \tau^2}$$

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Effect of finite formation time cont.



Effect of finite formation time cont.





Is the conclusion reliable?

Why the momentum configuration is important?

Seeds of instability

 $\langle j_a^{\mu}(x) \rangle = 0$ but current fluctuations are finite

$$\left\langle j_{a}^{\mu}(x_{1}) j_{b}^{\nu}(x_{2}) \right\rangle = \frac{1}{8} \delta^{ab} \int \frac{d^{3}p}{(2\pi)^{3}} \frac{p^{\mu}p^{\nu}}{E_{p}^{2}} f(\mathbf{p}) \delta^{(3)}(\mathbf{x} - \mathbf{v}t) \neq 0$$

$$x_1 = (t_1, \mathbf{x}_1), \quad x_2 = (t_2, \mathbf{x}_2), \quad x = (t_1 - t_2, \mathbf{x}_1 - \mathbf{x}_2)$$



Direction of the momentum surplus

Mechanism of filamentation



Isotropization - particles





Isotropization - fields



$$\begin{array}{c} \hline \mathbf{E} \\ \hline \mathbf{E} \\ \hline \mathbf{K} \\ \otimes \odot \\ \mathbf{B} \end{array} \end{array} \mathbf{k} \quad \mathbf{P}_{fields} \sim \mathbf{B}^{a} \times \mathbf{E}^{a} \sim \mathbf{k} \\ \end{array}$$

Prolate vs. oblate

