

# Torque (pokrętność)

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[research with P. Bożek, J. Moreira (PRC 83 (2011) 034911), A. Olszewski]

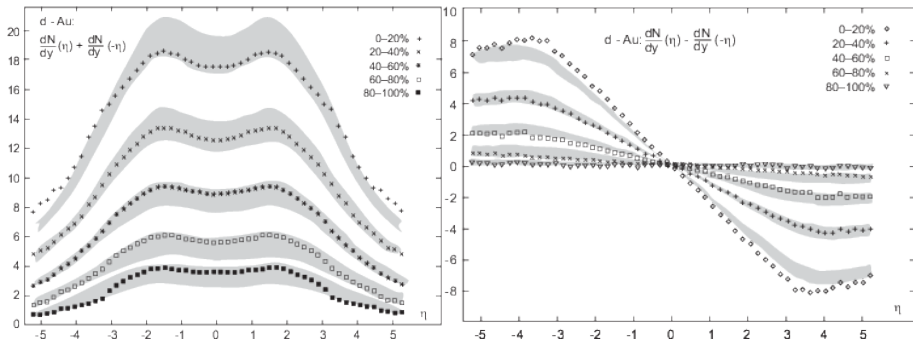
## Correlations in rapidity

- Info on earliest stages
- Sensitivity to production mechanism
- Terra incognita
- On-going e-by-e studies

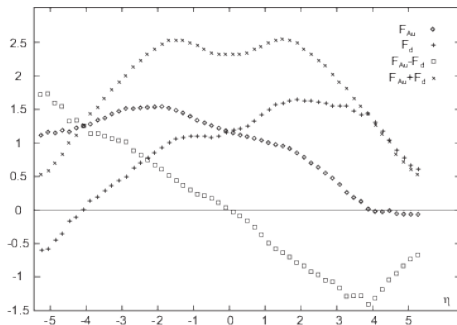
## Outline

- Emission “triangles”
- Fluctuations → torque effect
- Decorrelation effects on freeze-out
- Measures of torque
- Principal Component Analysis

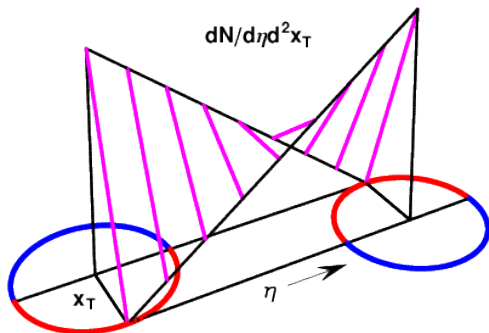
# Białas & Czyż: d-Au from PHOBOS



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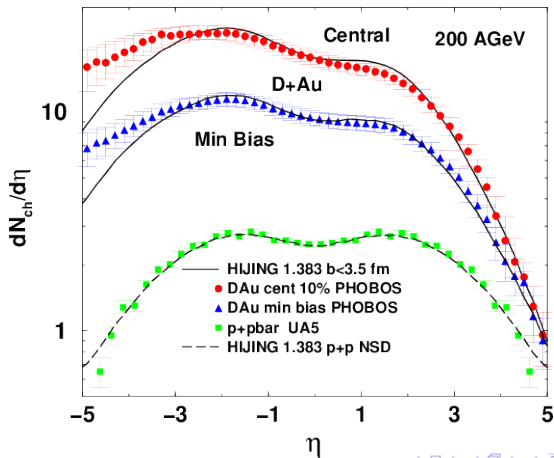


[Białas, Jeżabek (2004), Fiałkowski, Wit (2005), Adil, Gyulassy (2005)A. Adil, Gaździcki, Gorenstein (2006), Bzdak (2009), Białas, Zalewski (2010), Bzdak, Woźniak (2010), Bożek, Wyskiel (2010)]



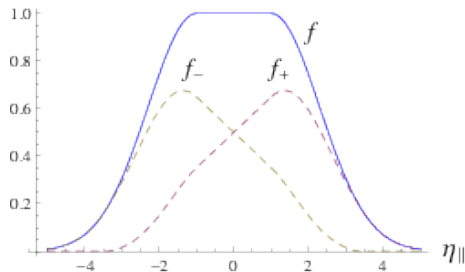
[Adil, Gyulassy]

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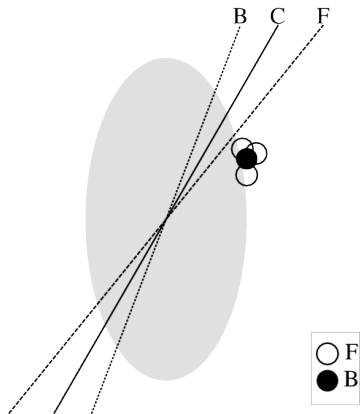
# Parametrization (Bożek)

Initial (partonic) density:



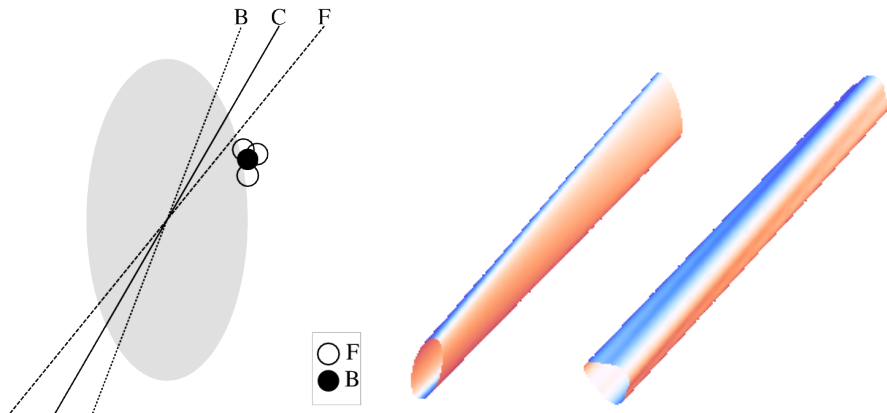
(for highest RHIC energy)

# The torque effect



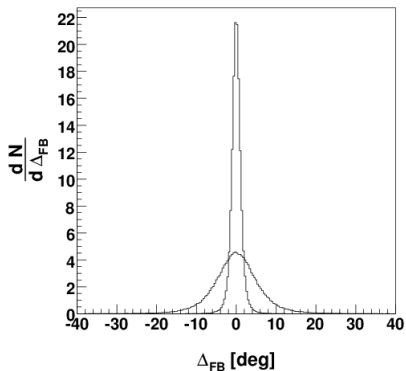


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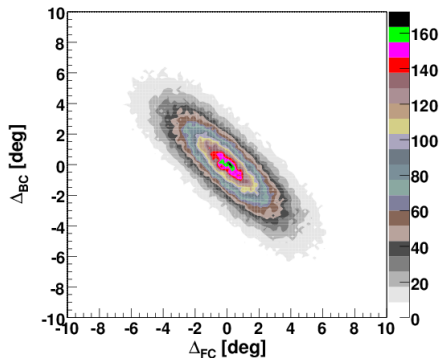
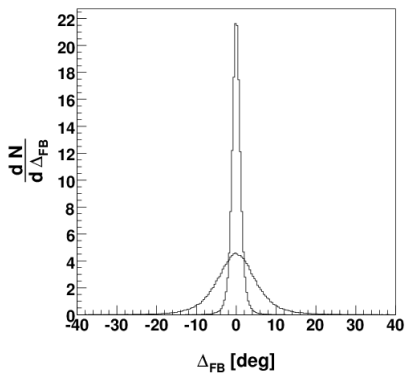
$$\Psi(k) = \frac{1}{k} \arctan \left( \frac{\sum_{i=1}^n w_i r_i^2 \sin(k\phi_i)}{\sum_{i=1}^n w_i r_i^2 \cos(k\phi_i)} \right)$$

# The torque effect



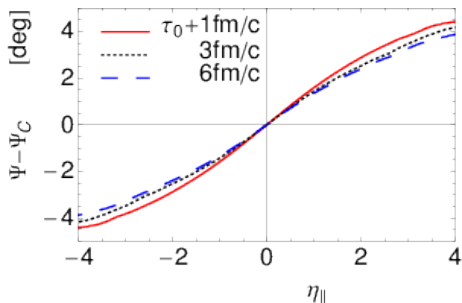
Distribution of the difference of the forward and backward torque angles for the elliptic deformation. The narrower and wider distributions correspond  $\Delta\eta_{||} = 1$  and 5, respectively. Centrality 20-30%, mixed model for Au+Au collisions with  $\alpha = 0.145$

# The torque effect



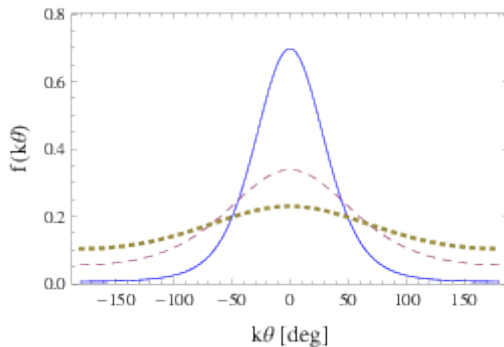
Right: 2D distribution of the relative torque angles  $\Delta_{FB}$  and  $\Delta_{FC}$  for centrality 50-60% and  $\Delta\eta_{||} = 5$ . The correlation coefficient is -0.61

Assumed deterministic evolution down to freeze-out  $\rightarrow$  correlations survive



# Statistical hadronization

Finite no. of particle in a  $\Delta\eta$  bin  $\rightarrow$  fluctuations of the principal angle  $\Theta$



e-by-e distribution of  $k\Theta$ ,  $k = 2, 3, \dots$ , for  $v_k = 5\%$  for several values of the event multiplicity  $n$ : 600 (solid), 100 (dashed), and 20 (dotted).

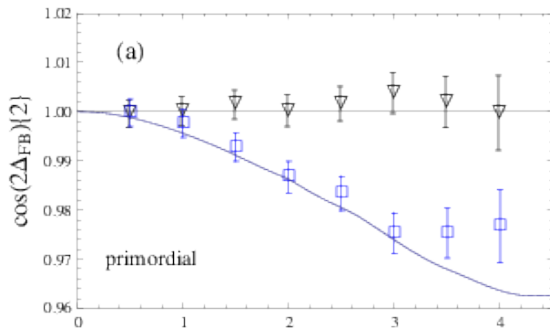
$$\cos(k\Delta_{FB}) \{2\} \equiv \frac{\langle e^{ik(\phi_F - \phi_B)} \rangle}{\sqrt{\langle e^{ik(\phi_{F,1} - \phi_{F,2})} \rangle \langle e^{ik(\phi_{B,1} - \phi_{B,2})} \rangle}} = \langle \cos(k\Delta_{FB}) \rangle_{\text{events}} + \text{nonflow.}$$

$$\cos(2k\Delta_{FB}) \{4\} \equiv \frac{\langle e^{ik[(\phi_{F,1} + \phi_{F,2}) - (\phi_{B,1} + \phi_{B,2})]} \rangle}{\langle e^{ik[(\phi_{F,1} - \phi_{F,2}) - (\phi_{B,1} - \phi_{B,2})]} \rangle} = \langle \cos(2k\Delta_{FB}) \rangle_{\text{events}} + \text{nonflow}$$

$$\langle e^{in(\phi_F - \phi_B)} \rangle = \frac{1}{N_{\text{events}}} \sum_{\text{events}} \frac{1}{n_F n_B} \sum_{i=1}^{n_F} \sum_{j=1}^{n_B} e^{ik(\phi_i - \phi_j)}$$

Results (one hydro event from averaged condition,  
 $c = 20 - 25\%$ )

Primordial particles (no resonance decays):

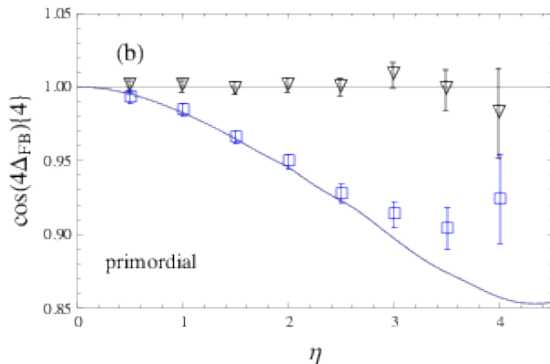


triangles – no torque, squares – torque

line – fireball torque angle after hydro (no hadronization)

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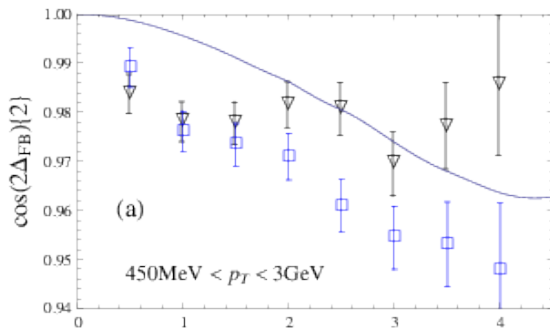
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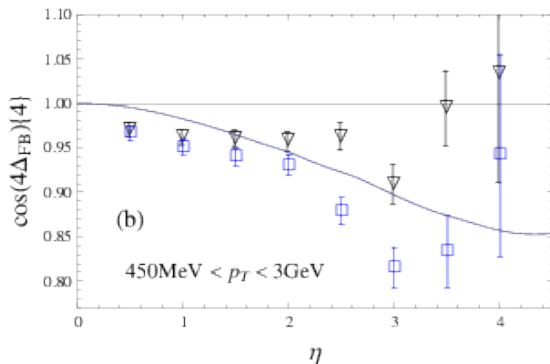
# Results (one hydro event from averaged condition, $c = 20 - 25\%$ )

Physical particles (with resonance decays):



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# Principle Component Analysis (PCA)

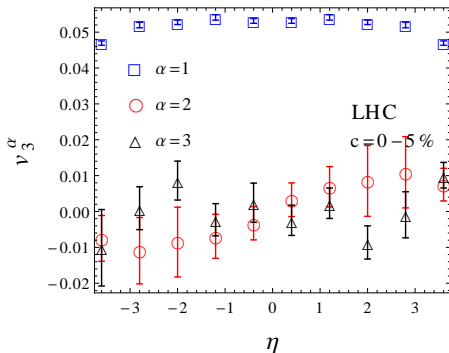
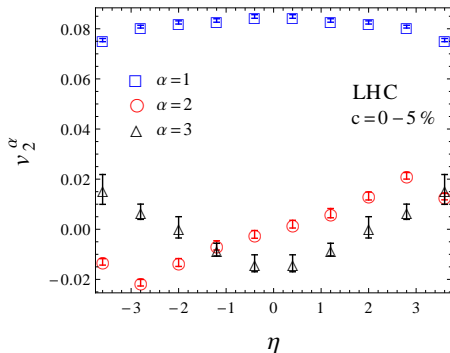
[standard multivariate method,  
recalled by Bhalerao, Ollitrault, Pal, Teaney (2014)]

- Take  $N$  bins
- Evaluate  $N \times N$  covariance matrix  $\rho$
- Find eigenvectors and eigenvalues (principal system)
- If  $\lambda_i \gg \lambda_j \rightarrow$  mode  $i$  much more collective than  $j$

[white board drawings, relation to torque]

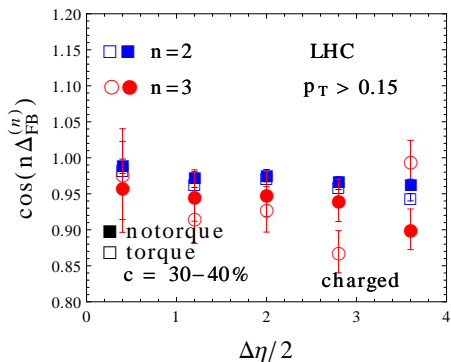
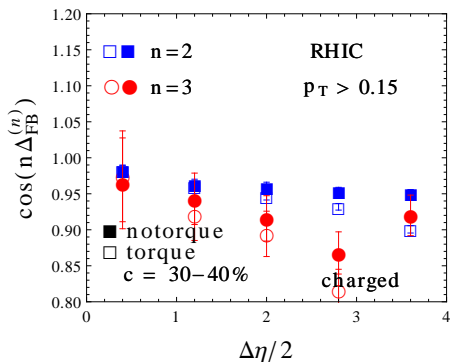
# Results from PCA (sneak preview of AO work)

[work with P. Bożek and AO]



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- Torque (FB flow correlations) ARE presently studied at LHC
- Origin: initial “triangles” and fluctuations
- Decorrelation from hadronization needs to be carefully analyzed (no-torque adds to torque)

(to be continued by AO)