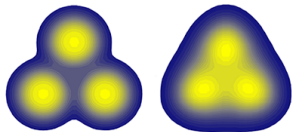


Struktura lekkich jąder z ultrarelatywistycznych zderzeń

Wojciech Broniowski

Kawiory

21 III 2014



[szczegóły w WB& E. Ruiz Arriola, *arXiv:1312.0289*, PRL 112, 112501]

NEWS AND COMMENTARY IN PHYSICS:

An Untested Window into Nuclear Structure, <http://journals.aps.org/prl/>

Instead of outline

(WPCF 2013 in Catania $\rightarrow \alpha$)

Two phenomena are related:

α clustering in light nuclei



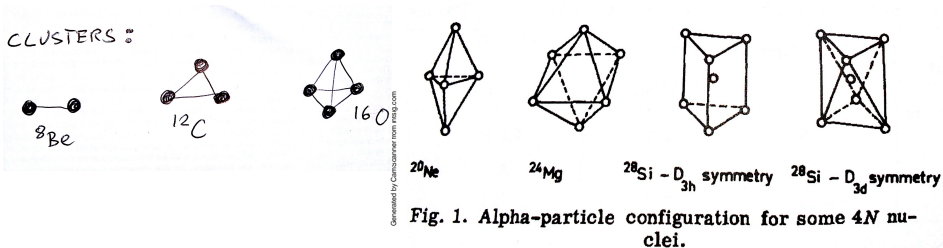
harmonic flow in ultra-relativistic A+B collisions

Surprising link:

low-energy structure \longleftrightarrow highest energy reactions

Some history

David Brink: After Gamow's theory of α -decay it was natural to investigate a model in which nuclei are composed of α -particles. Gamow developed a rather detailed theory of properties in his book "Constitution of Nuclei" published in 1931 before the discovery of the neutron in 1932. He supposed that $4n$ -nuclei like ${}^8\text{Be}$, ${}^{12}\text{C}$, ${}^{16}\text{O}$... were composed of α -particles



Shell model and its problems

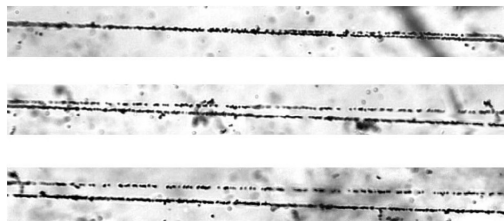
Michael P. Carpenter: *However, in the 1960s, excited states in nuclei that comprise equal numbers of protons and neutrons, (e.g., ^{12}C and ^{16}O) were identified that could not be described by the shell model, and it was suggested by Ikeda and others that these states could be associated with configurations composed of α particles*

Also: problems with α decay of ^{212}Po
shell model predicts a way too small decay width
spectroscopy: $^{212}\text{Po} = ^{208}\text{Pb} + \alpha$ [Astier et al. 2014]

Fragmentation

Evidence from dissociation in nuclear track emulsions

[Zarubin 2013 (BECQUEREL)]



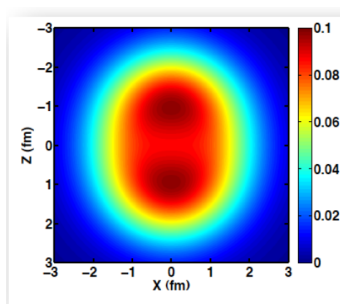
Example: dissociation of ${}^7\text{Li}$ (energy of a few A GeV)

channel	${}^4\text{He}+{}^3\text{He}$	${}^3\text{He}+{}^3\text{He}$	${}^4\text{He}+2p$	${}^4\text{He}+d+p$	${}^3\text{He}+2p$	${}^3\text{He}+d+p$	${}^3\text{He}+2d$	${}^3\text{He}+t+p$	$3p+d$	${}^6\text{Li}+p$
N	30	11	13	10	9	8	1	1	2	9
%	31	12	14	11	10	9	1	1	2	10

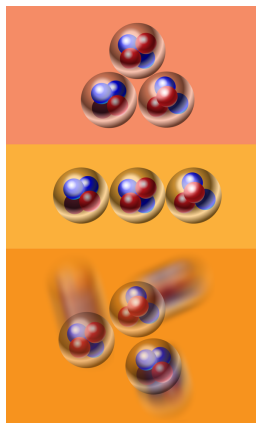
Numerous ongoing experiments (GANIL, Osaka, ...)

However, these studies cannot reveal the geometry (cluster arrangement)

Present theory status



${}^9\text{Be}$



${}^{12}\text{C}$

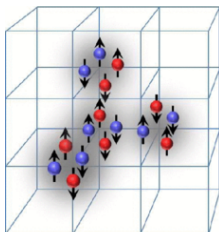
ground

Hoyle 0^+

other excited, 2^+ ...

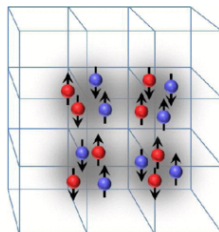
[M. Freer: WPCF13, H. Fynbo+Freer: Physics 4 (2011) 94]

Ab initio calculations of ^{16}O with chiral NN force (Juelich 2014)
→ strong α clusterization



(a) Initial state "A",
8 equivalent orientations.

ground state



(b) Initial states "B" and "C",
3 equivalent orientations.

excited

Numerical techniques

Funaki et al.: *certain states in self-conjugated nuclei ... can be described as product states of α particles, all in the lowest $0S$ state. We define a state of condensed α particles in nuclei as a bosonic product state in good approximation, in which all bosons occupy the lowest quantum state of the corresponding bosonic mean-field potential (α BEC)*

Another approach: Fermionic Molecular Dynamics (FMD)

A=2-12:

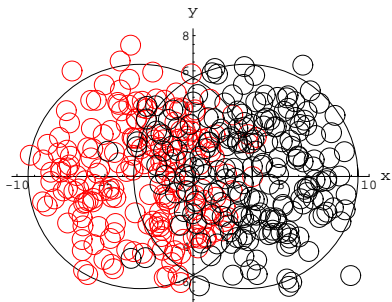
Quantum Variational Monte Carlo (with 2- and 3-body forces)

[R. Wiringa et al., <http://www.phy.anl.gov/theory/research/density/>]

All approaches to light nuclei give clusters

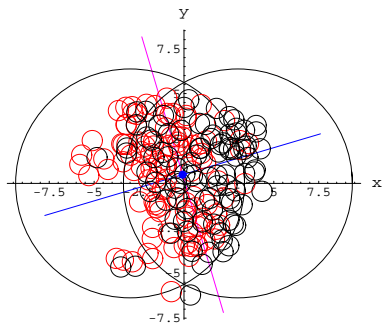
Goal (not yet accurately reached):

reproduce ground-state energy, excitation spectrum, EM form factor, ...



Au+Au collision at RHIC

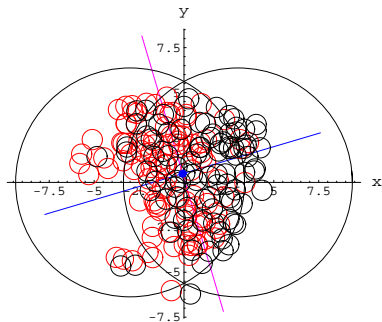
Participants:



- initial fireball is asymmetric in the transverse plane from 1) geometry 2) fluctuations
- **collectivity!** – **flow generated**
- strong elliptic flow, triangular flow from fluctuations, higher-order flow

“Initial shape – final flow” **transmutation** detectable in the asymmetry of the momentum distribution of detected particles

Participants:



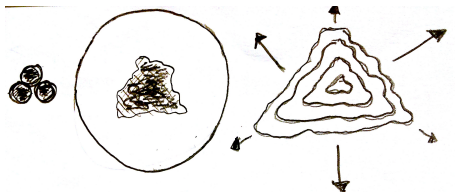
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“Initial shape – final flow” **transmutation** detectable in the asymmetry of the momentum distribution of detected particles

Merge the two ideas (α 's and flow) →

From α clusters to flow in relativistic collisions

α clusters \rightarrow asymmetry of shape \rightarrow asymmetry of initial fireball \rightarrow
 \rightarrow hydro or transport \rightarrow collective harmonic flow



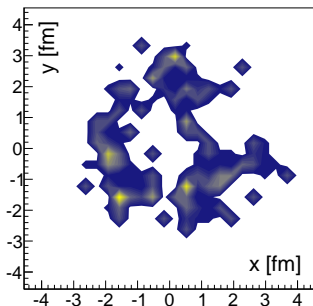
nuclear triangular geometry \rightarrow fireball triangular geometry \rightarrow triangular flow

What are the signatures, chances of detection?

Related idea: triton/ ^3He -Au at RHIC in 2015 [Sickles (PHENIX) 2013]
The case of light nuclei is more promising, as it leads to abundant fireballs

why ultrarelativistic?

reaction time is much shorter than time scales of the structure
→ a frozen “snapshot” of the nuclear configuration

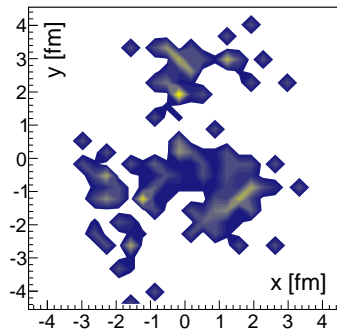


$$(N_w > 70)$$

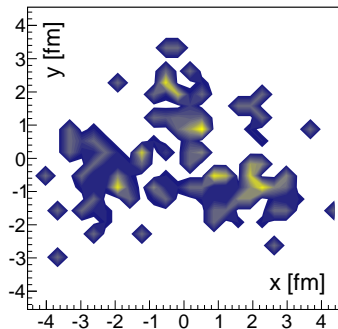
Imprints of the three α clusters clearly visible

[simulations with GLISSANDO 2]

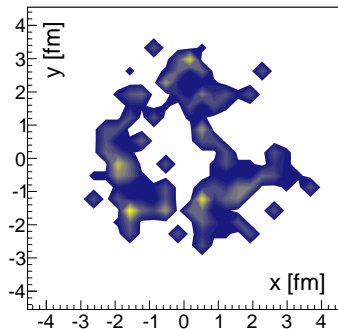
... more events



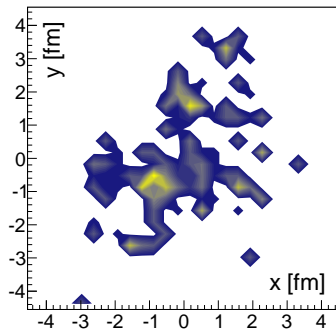
... more events



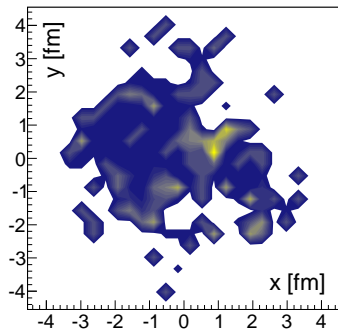
... more events



... more events



... more events



The meaning of *intrinsic*

Ground-state nuclei are (mostly) in 0^+ states (rotationally symmetric wave functions). The meaning of *deformation* concerns **multiparticle correlations** between the nucleons

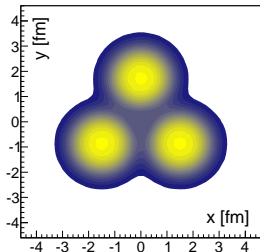
Superposition over orientations:

$$|\Psi_{0^+}(x_1, \dots, x_N)\rangle = \frac{1}{4\pi} \int d\Omega \Psi_{\text{intr}}(x_1, \dots, x_N; \Omega)$$

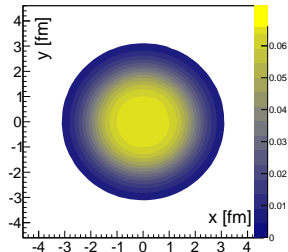
(holds from deuterium to U)

The *intrinsic* density of sources of rank n is defined as the average over events, where the distributions in each event have aligned principal axes: $f_n^{\text{intr}}(\vec{x}) = \langle f(R(-\Phi_n)\vec{x}) \rangle$. Brackets indicate averaging over events and $R(-\Phi_n)$ is the inverse rotation by the principal-axis angle in each event

Intrinsic distributions in ^{12}C : three α 's in a triangular arrangement

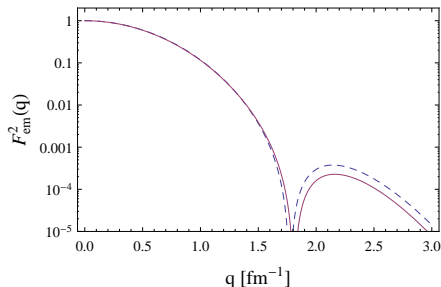
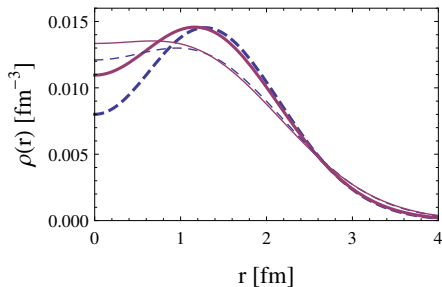


clustered



unclustered

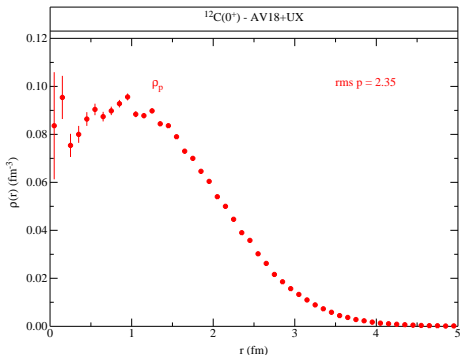
Constraints from EM form factor



Electric charge density (thin lines) and the corresponding distribution of the centers of protons (thick lines) in ^{12}C for the data and BEC calculations (dashed lines), and for the FMD calculations (solid lines), plotted against the radius. **BEC agrees with the experimental data**

Central depletion from the hole between the clusters

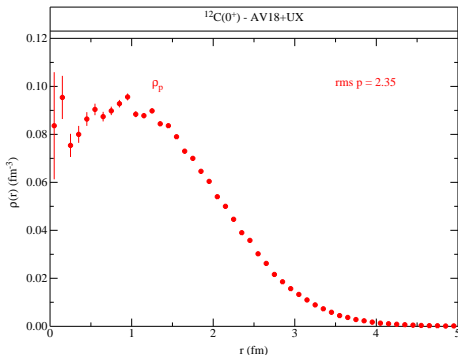
^{12}C from Wiringa



Distribution of the centers of protons = neutrons in ^{12}C

Central depletion

^{12}C from Wiringa



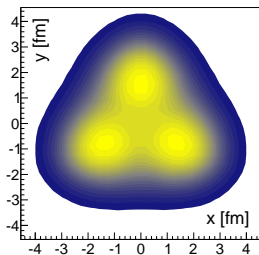
Distribution of the centers of protons = neutrons in ^{12}C

Central depletion

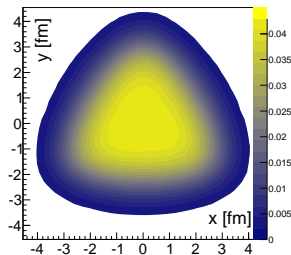
Have good MC distributions \rightarrow carry out detailed simulations

Mixed Glauber model at SPS conditions: $n \sim \frac{1-a}{2}N_w + aN_{\text{bin}}$, $a = 0.12$

Intrinsic distributions in the *transverse plane* of the fireball with $N_w > 70$
– large multiplicity

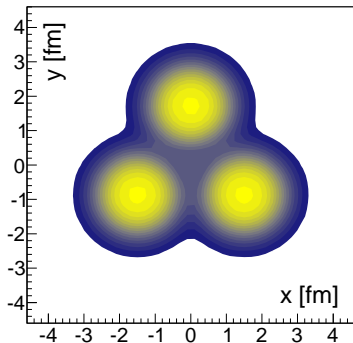


clustered



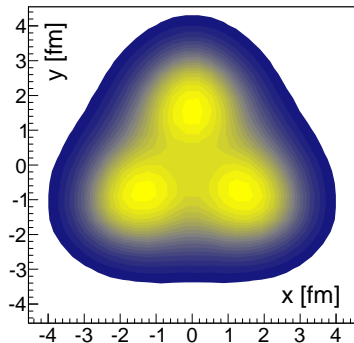
unclustered

Geometry of nucleus \rightarrow geometry of fireball



intrinsic density of ^{12}C

\rightarrow



geometry of the fireball

Eccentricity parameters

Eccentricity parameters ϵ_n ,

$$\epsilon_n e^{in\Phi_n} = \frac{\sum_j \rho_j^n e^{in\phi_j}}{\sum_j \rho_j^n},$$

describe the shape of each event (j labels the sources in the event, n =rank, Φ_n is the principal axis angle)

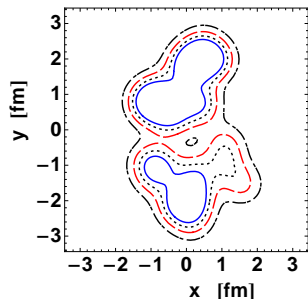
Two components:

- intrinsic (from existent mean deformation of the fireball)
- from fluctuations

Digression: d-Pb by Bożek

The deuteron has an intrinsic dumbbell shape with very large deformation: $r_{\text{rms}} \simeq 2$ fm

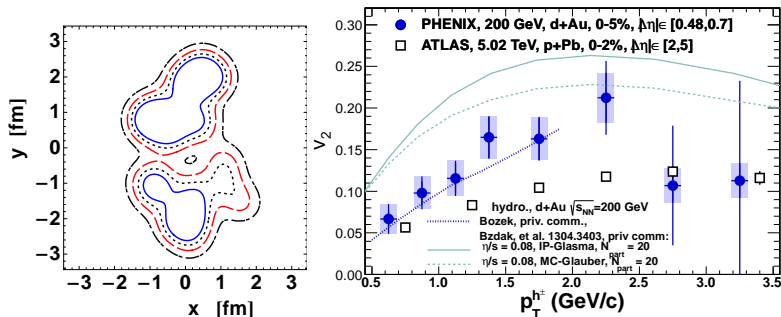
Initial entropy density in a d-Pb collision with $N_{\text{part}} = 24$ [Bożek 2012]



Digression: d-Pb by Božek

The deuteron has an intrinsic dumbbell shape with very large deformation: rms $\simeq 2$ fm

Initial entropy density in a d-Pb collision with $N_{\text{part}} = 24$ [Božek 2012]



Resulting large elliptic flow confirmed with the later RHIC data

Geometry vs multiplicity correlations in ^{12}C -Pb

A very specific feature of the ^{12}C collisions:

The cluster plane parallel or perpendicular to the transverse plane:

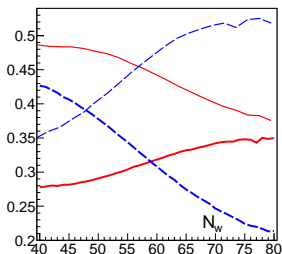


higher multiplicity
higher triangularity
lower ellipticity

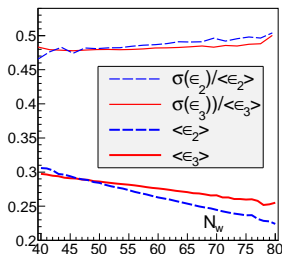


lower multiplicity
lower triangularity
higher ellipticity

Ellipticity and triangularity vs multiplicity



clustered



unclustered

Clusters:

When $N_w \nearrow$ then $\langle \epsilon_3 \rangle \nearrow$ and $\langle \epsilon_2 \rangle \searrow$

and $\langle \sigma(\epsilon_3) / \epsilon_3 \rangle \searrow$, $\langle \sigma(\epsilon_2) / \epsilon_2 \rangle \nearrow$ tending to $\sqrt{4/\pi - 1} \sim 0.52$

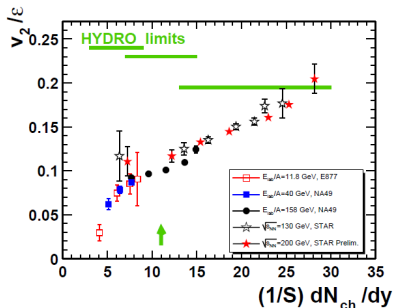
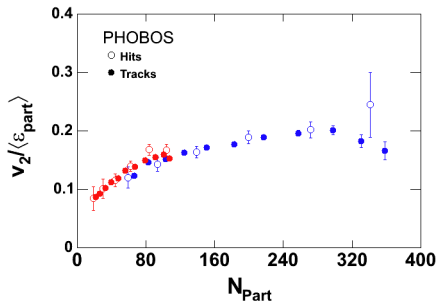
No clusters:

similar behavior for $n = 2$ and $n = 3$

Shape-flow transmutation

The eccentricity parameters are transformed (in all models based on collective dynamics) into asymmetry of the transverse-momentum flow. It has been found that

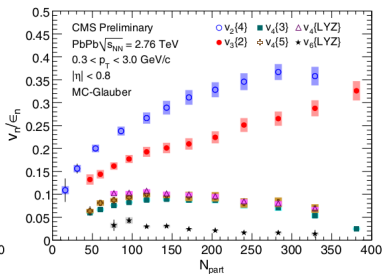
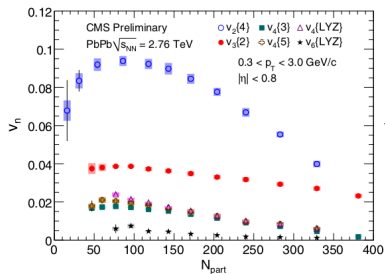
$\langle v_n \rangle$ grows with $\langle \epsilon_n \rangle$



Shape-flow transmutation

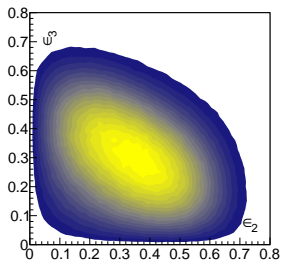
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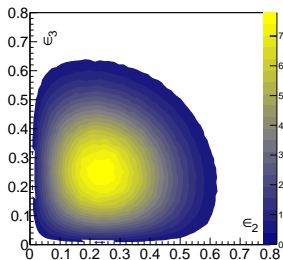


→ for ^{12}C collisions v_3 will grow with multiplicity even stronger than ϵ_3

Triangularity vs ellipticity



clustered

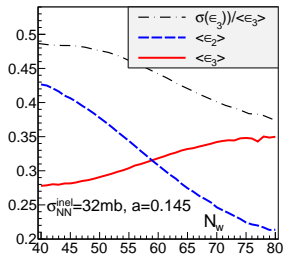


unclustered

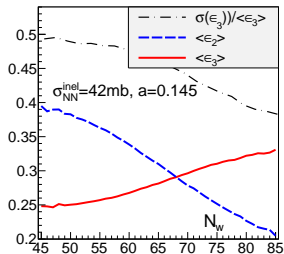
Clusters:

Anticorrelation: $\rho(\epsilon_2, \epsilon_3) \simeq -0.3$

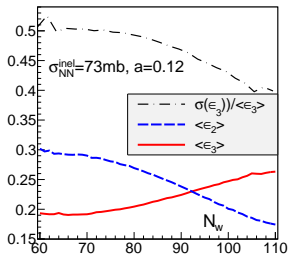
Dependence on the collision energy



32mb (SPS)



42mb (RHIC)



72mb (LHC)

Qualitative conclusions hold from SPS to the LHC

Why small on big?

small on big

small nucleus \rightarrow large deformation from clusters

big nucleus \rightarrow large fireball, collectivity

small on small

more difficult evolution / particle production, other signatures if any

big on big

(U+U, Cu+Au) \rightarrow possible signatures of nuclear deformation (but not clustering) [Filip, Volshin 2010, Rybczyński, WB, Stefanek 2011]

ultrarelativistic \rightarrow snapshots

New method: nuclear structure snapshots from ultra-fast heavy ion collisions / Geometry of the ground st. → flow

Signatures (qualitative and quantitative) of clustered ^{12}C - ^{208}Pb collisions

- Increase of ϵ_3 and v_3 with multiplicity for the highest multiplicity events
- Decrease of scaled variance ϵ_3 and v_3 with multiplicity for the highest multiplicity events
- Anticorrelation of ϵ_2 and ϵ_3 , or v_2 and v_3

Extensions

- Other systems and other possible signatures (work in progress)
- More detailed modeling (involving hydrodynamics)

Possible future data (NA61, RHIC?) in conjunction with a detailed knowledge of the dynamics of the evolution of the fireball would allow to place constraints on the α -cluster structure of the colliding nuclei. Conversely, the knowledge of the clustered nuclear distributions may help to verify the fireball evolution models