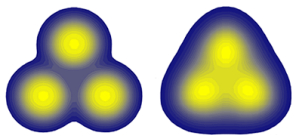


Nowe okno na strukturę lekkich jąder: klastry α a ultrarelatywistyczne zderzenia jądrowe

Wojciech Broniowski

IFJ PAN

24 IV 2014



[szczegóły w WB& E. Ruiz Arriola, *arXiv:1312.0289*, PRL 112, 112501]

Two phenomena are related:

α clustering in light nuclei



harmonic flow in ultra-relativistic A+B collisions

Surprising link:

low-energy structure \longleftrightarrow highest energy reactions

α clusters

Some history

David Brink: After Gamow's theory of α -decay it was natural to investigate a model in which nuclei are composed of α -particles. Gamow developed a rather detailed theory of properties in his book "Constitution of Nuclei" published in 1931 before the discovery of the neutron in 1932. He supposed that $4n$ -nuclei like ${}^8\text{Be}$, ${}^{12}\text{C}$, ${}^{16}\text{O}$... were composed of α -particles

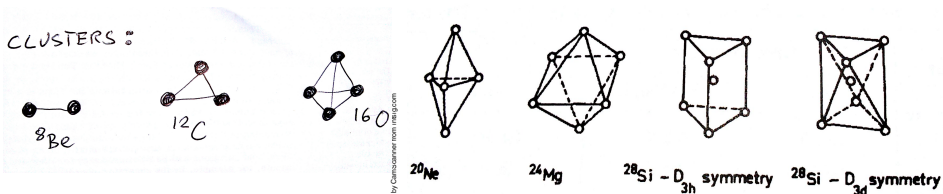
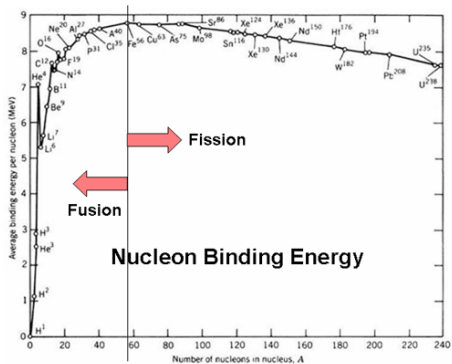


Fig. 1. Alpha-particle configuration for some $4N$ nuclei.

Generated by CamScanner from intsig.com

Binding



α very tightly bound

Shell model (and its problems)

Eugene Wigner, Maria Goeppert-Mayer, Hans Jensen, Nobel in 1963

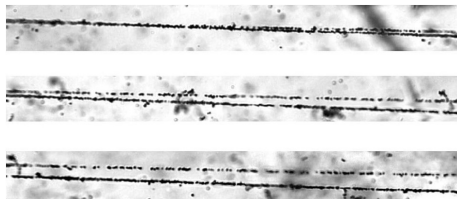
Michael P. Carpenter: *However, in the 1960s, excited states in nuclei that comprise equal numbers of protons and neutrons, (e.g., ^{12}C and ^{16}O) were identified that could not be described by the shell model, and it was suggested by Ikeda and others that these states could be associated with configurations composed of α particles*

Also: problems with α decay of ^{212}Po
shell model predicts a way too small decay width
spectroscopy: $^{212}\text{Po} = ^{208}\text{Pb} + \alpha$ [Astier et al. 2014]

Fragmentation

Evidence from dissociation in nuclear track emulsions

[Zarubin 2013 (BECQUEREL)]



Example: dissociation of ${}^7\text{Be}$ (energy of a few A GeV)

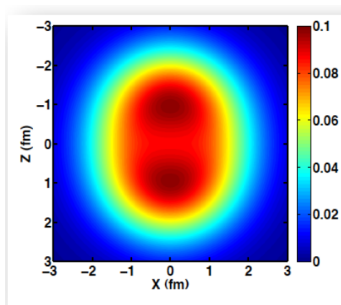
channel	${}^4\text{He}+{}^3\text{He}$	${}^3\text{He}+{}^3\text{He}$	${}^4\text{He}+2p$	${}^4\text{He}+d+p$	${}^3\text{He}+2p$	${}^3\text{He}+d+p$	${}^3\text{He}+2d$	${}^3\text{He}+t+p$	$3p+d$	${}^6\text{Li}+p$
N	30	11	13	10	9	8	1	1	2	9
%	31	12	14	11	10	9	1	1	2	10

Numerous ongoing experiments (GANIL, Osaka, ...)

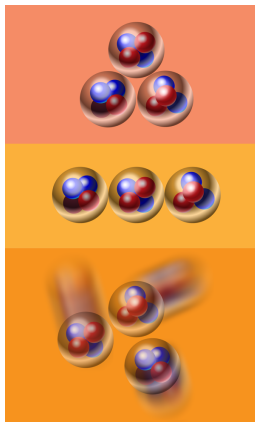
Was the cluster there or is it created at break-up?

These studies cannot reveal the geometry (cluster arrangement)

Present theory status



${}^9\text{Be}$



${}^{12}\text{C}$

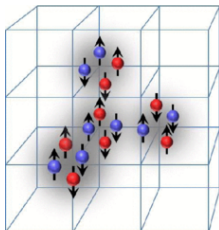
ground

Hoyle 0^+

other excited, 2^+ ...

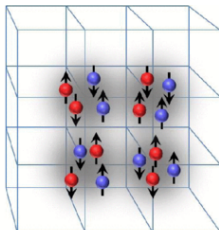
[M. Freer: WPCF13, H. Fynbo+Freer: Physics 4 (2011) 94]

Ab initio calculations of ^{16}O with chiral NN force (Juelich 2014)
→ strong α clusterization



(a) Initial state "A",
8 equivalent orientations.

ground state



(b) Initial states "B" and "C",
3 equivalent orientations.

excited

Computational techniques

(massive effort)

Funaki et al.: *certain states in self-conjugated nuclei ... can be described as product states of α particles, all in the lowest $0S$ state. We define a state of condensed α particles in nuclei as a bosonic product state in good approximation, in which all bosons occupy the lowest quantum state of the corresponding bosonic mean-field potential (α BEC)*

Another approach: Fermionic Molecular Dynamics (FMD)

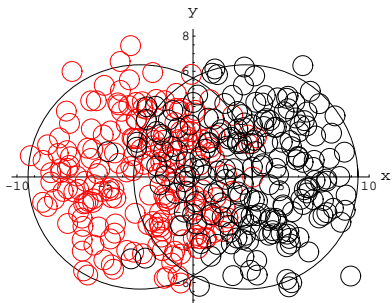
Quantum Variational Monte Carlo (with 2- and 3-body forces) for $A=2-12$
[R. Wiringa et al., <http://www.phy.anl.gov/theory/research/density/>]

All approaches to light nuclei give clusters

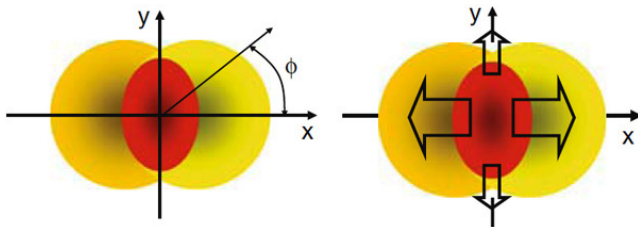
Goal (not yet accurately reached):

reproduce ground-state energy, excitation spectrum, EM form factor, ...

Flow

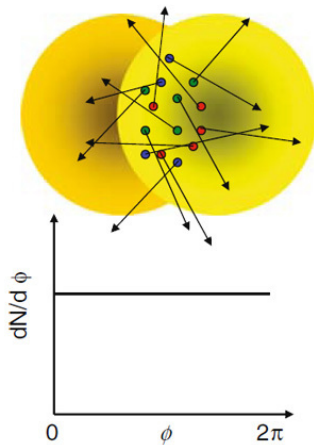
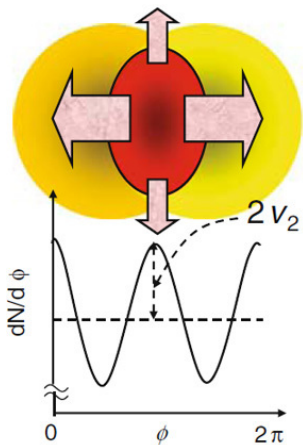


Au+Au collision at RHIC



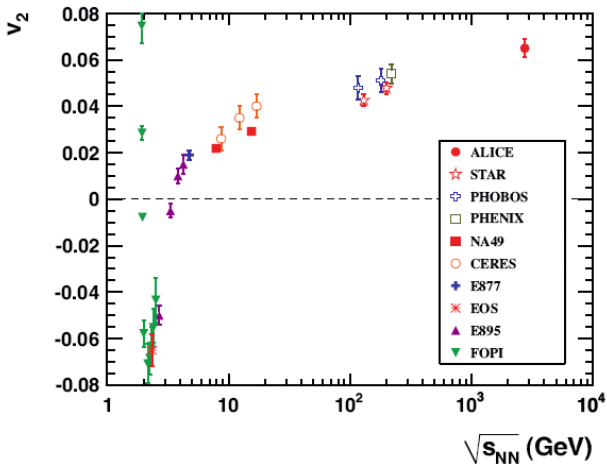
“Initial shape – final flow” transmutation detectable in the asymmetry of the momentum distribution of detected particles

Elliptic flow

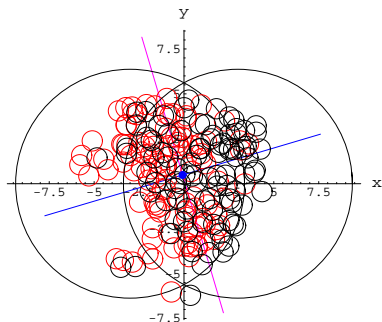


[ALICE]

Major observation in HIC – signature of QGP



Participants:

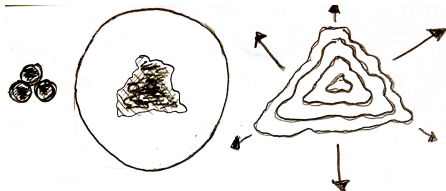


- initial fireball is asymmetric in the transverse plane from 1) geometry 2) fluctuations
- **collectivity!** – flow generated
- strong elliptic flow, triangular flow from fluctuations, higher-order flow

Merge the two ideas (α 's and flow) \rightarrow

From α clusters to flow in relativistic collisions

α clusters \rightarrow asymmetry of shape \rightarrow asymmetry of initial fireball \rightarrow
 \rightarrow hydro or transport \rightarrow collective harmonic flow



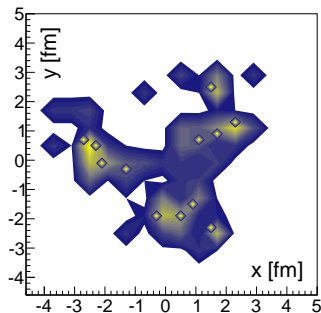
nuclear triangular geometry \rightarrow fireball triangular geometry \rightarrow triangular flow

What are the signatures, chances of detection?

Related idea: triton/ ^3He -Au at RHIC in 2015 [Sickles (PHENIX) 2013]
The case of light nuclei is more promising, as it leads to abundant fireballs

why ultrarelativistic?

reaction time is much shorter than time scales of the structure
→ a frozen “snapshot” of the nuclear configuration

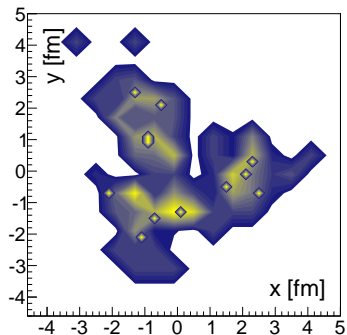


($N_w > 70$ - flat-on orientation)

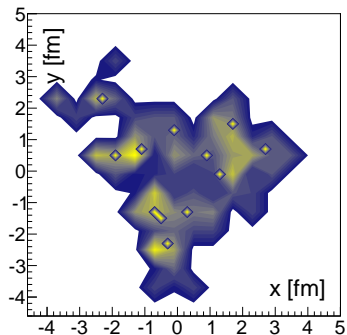
Imprints of the three α clusters clearly visible

[simulations with GLISSANDO 2]

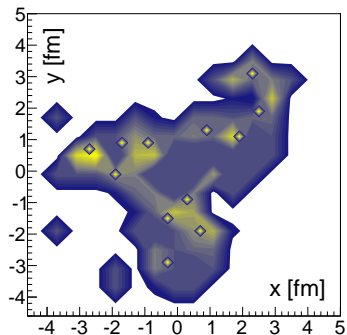
... more events



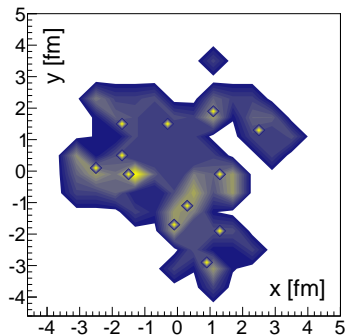
... more events



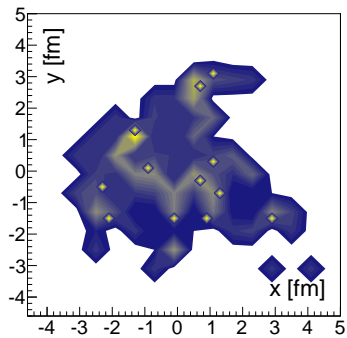
... more events



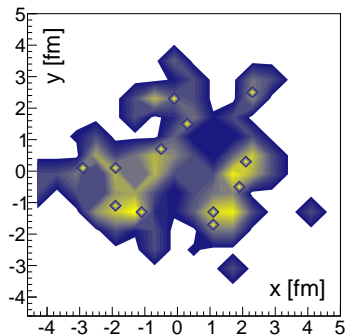
... more events



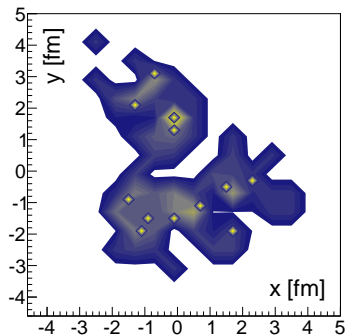
... more events



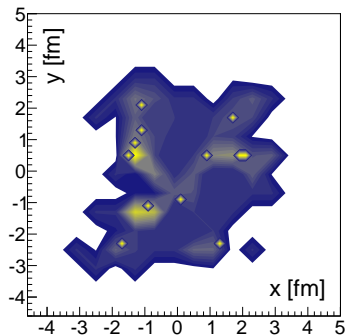
... more events



... more events



... more events



The meaning of *intrinsic*

Ground state of ^{12}C is a 0^+ state (rotationally symmetric wave function).
The meaning of *deformation* concerns **multiparticle correlations** between the nucleons

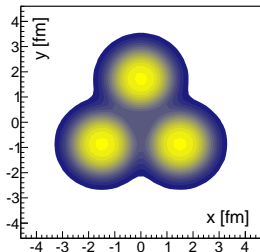
Superposition over orientations:

$$|\Psi_{0^+}(x_1, \dots, x_N)\rangle = \frac{1}{4\pi} \int d\Omega \Psi_{\text{intr}}(x_1, \dots, x_N; \Omega)$$

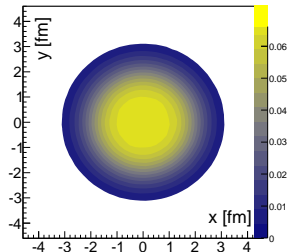
The *intrinsic* density of sources of rank n is defined as the average over events, where the distributions in each event have aligned principal axes:
 $f_n^{\text{intr}}(\vec{x}) = \langle f(R(-\Phi_n)\vec{x}) \rangle$. Brackets indicate averaging over events and $R(-\Phi_n)$ is the inverse rotation by the principal-axis angle in each event

Back to ^{12}C – intrinsic density

Intrinsic distributions in ^{12}C : three α 's in a triangular arrangement

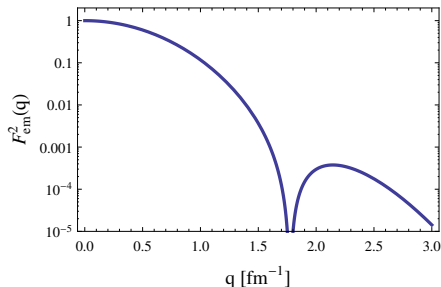
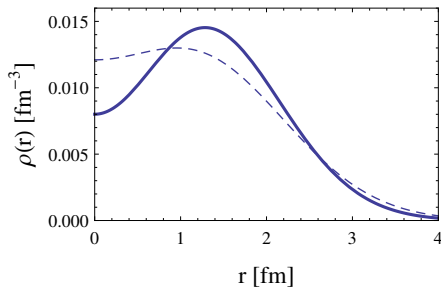


clustered



unclustered

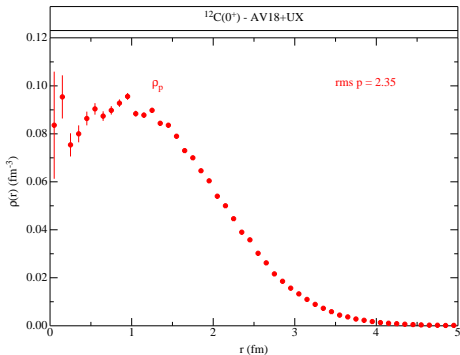
Constraints on ^{12}C from EM form factor



Electric charge density (dashed line) and the corresponding distribution of the centers of protons (solid line) in ^{12}C for the data plotted against the radius, for the **BEC** calculation – agrees with the experimental data for the charge form factor

Central depletion naturally explained with the hole between the clusters

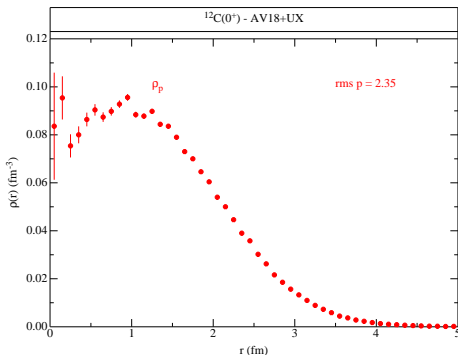
^{12}C from Wiringa's MC



Distribution of the centers of protons = neutrons in ^{12}C

smaller central depletion

^{12}C from Wiringa's MC



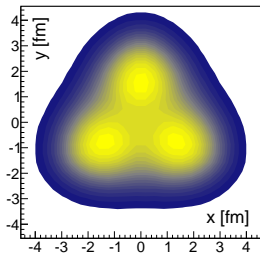
Distribution of the centers of protons = neutrons in ^{12}C

smaller central depletion

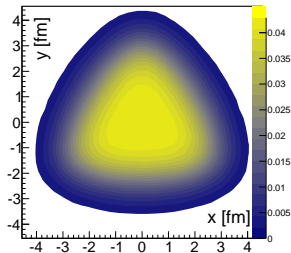
GLISSANDO implements these clustered distributions

→ carry out detailed simulations

Intrinsic distributions in the *transverse plane* of the fireball (here with $N_w > 70$ – large multiplicity enforcing the flat-on collision)

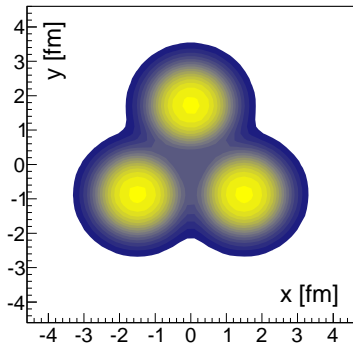


clustered



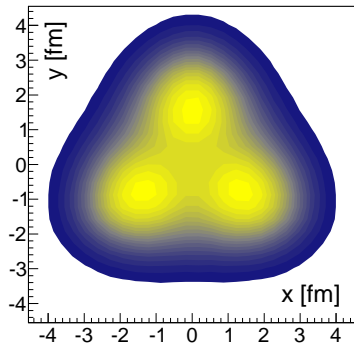
unclustered

Geometry of nucleus \rightarrow geometry of fireball



intrinsic density of ^{12}C

\rightarrow



geometry of the fireball

Eccentricity parameters ϵ_n (Fourier analysis)

$$\epsilon_n e^{in\Phi_n} = \frac{\sum_j \rho_j^n e^{in\phi_j}}{\sum_j \rho_j^n}$$

describe the shape of each event (j labels the sources in the event, n =rank, Φ_n is the principal axis angle)

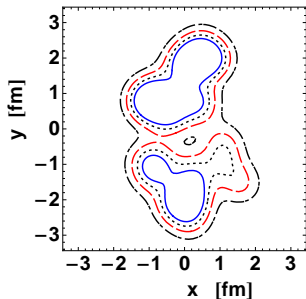
Two components:

- internal (from existent mean deformation of the fireball)
- from fluctuations

Digression: d-A by Bożek

The deuteron has an intrinsic dumbbell shape with very large deformation: $r_{\text{rms}} \simeq 2$ fm

Initial entropy density in a d-Pb collision with $N_{\text{part}} = 24$ [Bożek 2012]

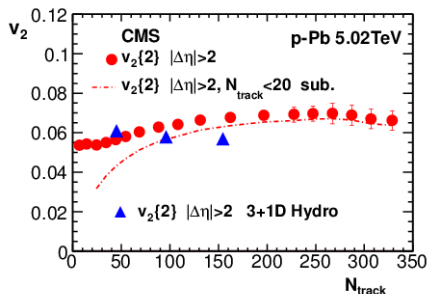


Resulting large elliptic flow confirmed with the later RHIC analysis

Digression 2: collectivity in small systems

Active research:

hydro in p-A, d-A collisions, pioneered by Bożek



[Bożek+WB+Torrieri PRL 111 (2013) 172303]

Geometry vs multiplicity correlations in ^{12}C -Pb

Specific feature of the ^{12}C collisions:

The cluster plane parallel or perpendicular to the transverse plane:

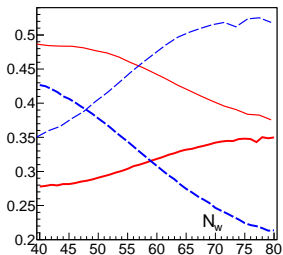


higher multiplicity
higher triangularity
lower ellipticity

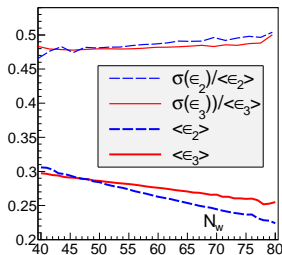


lower multiplicity
lower triangularity
higher ellipticity

Ellipticity and triangularity vs multiplicity



clustered



unclustered

Clusters:

When $N_w \nearrow$ then $\langle \epsilon_3 \rangle \nearrow$ and $\langle \epsilon_2 \rangle \searrow$

and $\langle \sigma(\epsilon_3)/\epsilon_3 \rangle \searrow$, $\langle \sigma(\epsilon_2)/\epsilon_2 \rangle \nearrow$ tending to $\sqrt{4/\pi - 1} \sim 0.52$

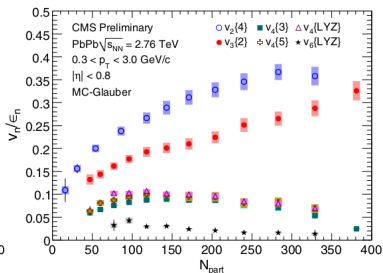
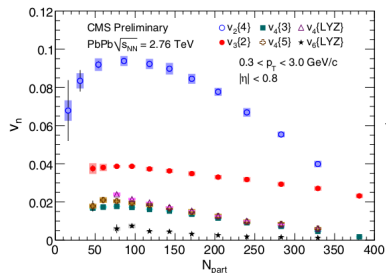
No clusters:

similar behavior for $n = 2$ and $n = 3$

Shape-flow transmutation

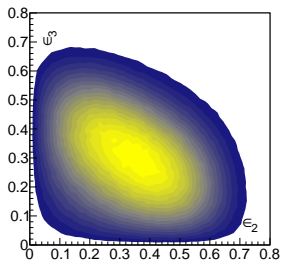
The eccentricity parameters are transformed (in all models based on collective dynamics) into asymmetry of the transverse-momentum flow
It has been found that

$\langle v_n \rangle$ grows with $\langle \epsilon_n \rangle$

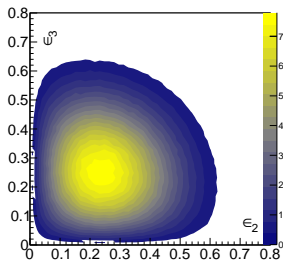


→ for ^{12}C collisions v_3 will grow with multiplicity even stronger than ϵ_3

Triangularity vs ellipticity



clustered

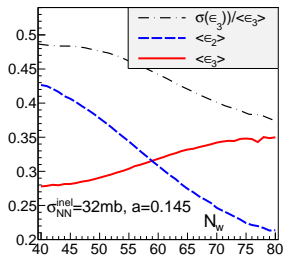


unclustered

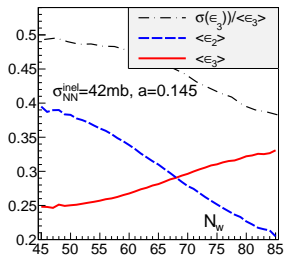
Clusters:

Anticorrelation: $\rho(\epsilon_2, \epsilon_3) \simeq -0.3$

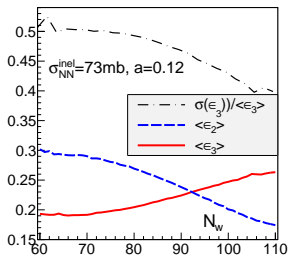
Dependence on the collision energy



32mb (SPS)



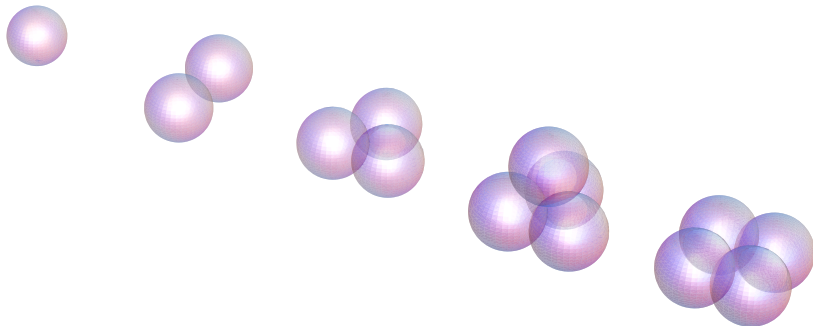
42mb (RHIC)



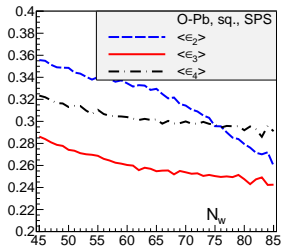
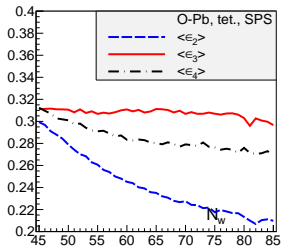
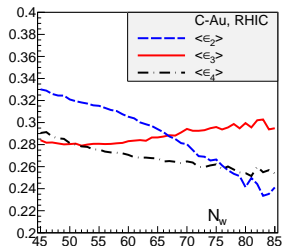
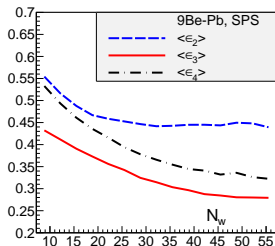
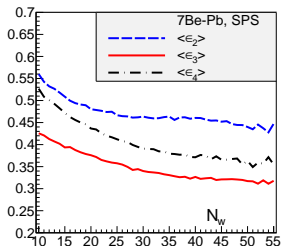
72mb (LHC)

Qualitative conclusions hold from SPS to the LHC

Other systems



Other systems (Wiringa's distributions)



[work with Maciej Rybczyński]

Conclusions

Why small on big?

small on big

small nucleus \rightarrow large deformation from clusters

big nucleus \rightarrow large fireball, collectivity

small on small

more difficult evolution / particle production, other signatures

big on big

(U+U, Cu+Au) \rightarrow possible signatures of nuclear deformation (but not clustering) [Filip, Voloshin 2010, Rybczyński, WB, Stefanek 2011]

ultrarelativistic \rightarrow snapshots

New method: nuclear structure from ultra-fast heavy ion collisions / Geometry of the ground state → flow

Signatures (qualitative and quantitative) of **clustered** ^{12}C - ^{208}Pb collisions

- Increase of triangularity with multiplicity for the highest multiplicity events
- Decrease of scaled variance of triangularity with multiplicity for the highest multiplicity events
- Anticorrelation of ellipticity and triangularity

Extensions (in progress)

- Other systems and other possible signatures
- More detailed modeling involving hydrodynamics

Possible future data (NA61, RHIC?) in conjunction with a detailed knowledge of the dynamics of the evolution of the fireball would allow to place constraints on the α -cluster structure of the colliding nuclei. Conversely, the knowledge of the clustered nuclear distributions may help to verify the fireball evolution models