

Hydro in small systems: How small can a QGP be?

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Initial Stages 2019
Columbia U., June 24–28, 2019

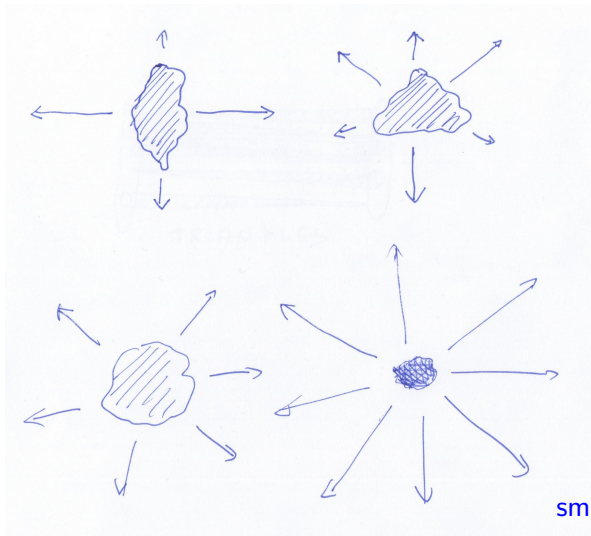
2015/19/B/ST2/00937

 NATIONAL SCIENCE CENTRE
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- More remarks on light-heavy collisions
 - see Monday talks by Schlichting, Mohapatra, Collab. reviews, parallel sessions
- Collisions with polarized light targets
- Collisions with light clustered nuclei

Remarks

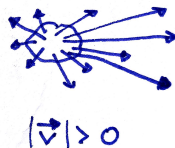
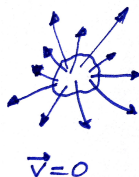
Shape – flow transmutation



Any (copious) rescattering will do (hydro, transport)!

Collimation from the Doppler effect

- Emission from a fast moving element of fluid
- Collimation of hadrons (increasing with mass)

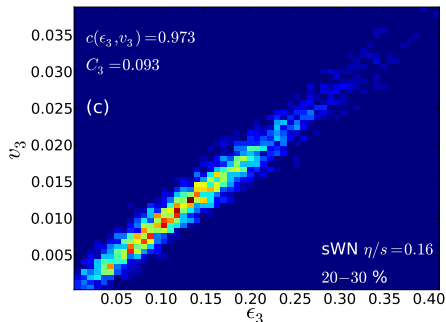
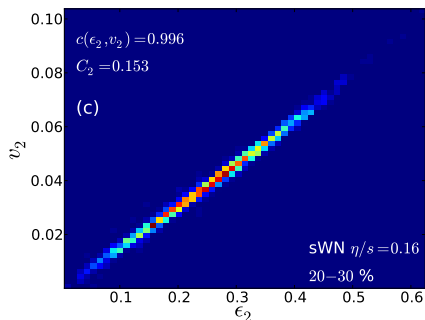


Multi-particle correlations in the azimuth are used in the **cumulant** or other methods to extract the flow coefficients with reduced the non-flow contamination (from jets, resonance decays, ...)

[Borghini, Ollitrault 2001]

Approximately $v_n = \kappa_n \epsilon_n$, ($n = 2, 3$)

- κ_n depend on the collision energy, multiplicity, viscosity ...



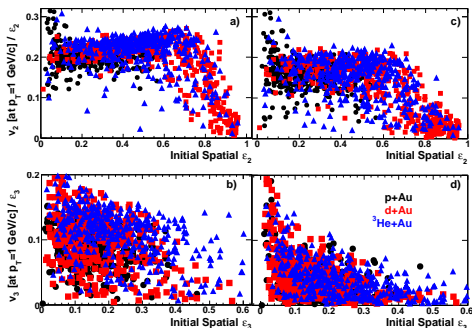
Au+Au@200 GeV [Niemi, Denicol, Holopainen, Huovinen 2012]

- cf. talk by Behera on Tuesday

Hydro without hydro

Approximately $v_n = \kappa_n \epsilon_n$, ($n = 2, 3$)

- κ_n depend on the collision energy, multiplicity, viscosity ...



$T_f = 150$ MeV (left) and 170 MeV (right) [Nagle, Adare, Beckman, Koblesky, Orjuela Koop, McGlinchey, Romatschke, Carlson, Lynn, McCumber, PRL 113 (2014) 112301]

- cf. talk by Behera on Tuesday

Approximately $v_n = \kappa_n \epsilon_n$, ($n = 2, 3$)

- κ_n depend on the collision energy, multiplicity, viscosity ...

Allows us to construct response-independent coefficients, e.g.,

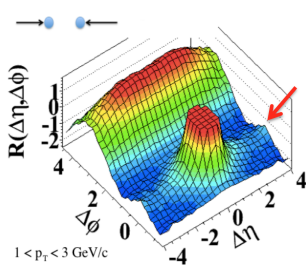
$$v_n\{4\}/v_n\{2\} \simeq \epsilon_n\{4\}/\epsilon_n\{2\}$$

which probe the geometry-fluctuation interplay
(more geometry $\rightarrow v_n\{4\}/v_n\{2\}$ goes up)

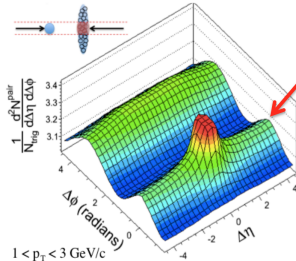
[Bożek WB, Ruiz Arriola, Rybczyński, 2014,
Giacalone, Noronha-Hostler, Ollitrault, 2017]

- cf. talk by Behera on Tuesday

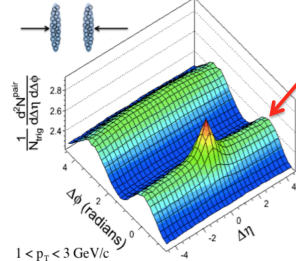
(a) pp $\sqrt{s} = 7$ TeV, $N_{\text{trk}}^{\text{offline}} \geq 110$



(b) pPb $\sqrt{s_{NN}} = 5.02$ TeV, $220 < N_{\text{trk}}^{\text{offline}} \leq 260$



(c) PbPb $\sqrt{s_{NN}} = 2.76$ TeV, $220 < N_{\text{trk}}^{\text{offline}} \leq 260$



Together with the transverse-longitudinal factorization, the near-side ridge indicates collectivity

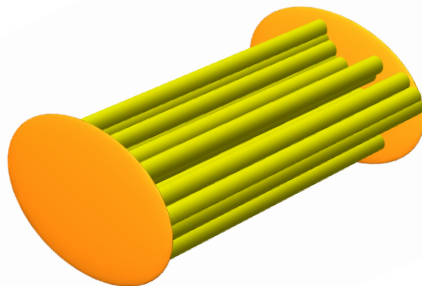
understanding of the ridges →

Factorization of the transverse and longitudinal distributions

left-moving participants

strings

right-moving participants

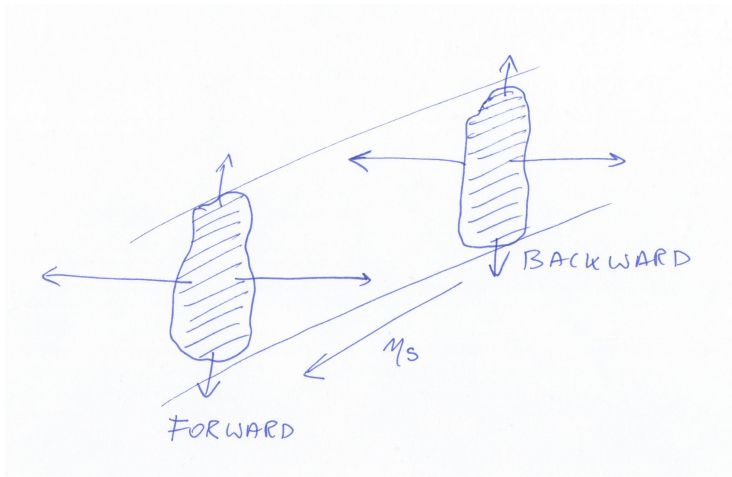


Factorization of the transverse and longitudinal distributions

left-moving participants

strings

right-moving participants



Approximate (up to fluctuations) alignment of F and B event planes

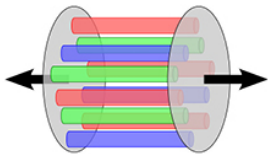
Collimation of flow at very distant longitudinal separations \rightarrow ridges!

Surfers - the near-side ridge



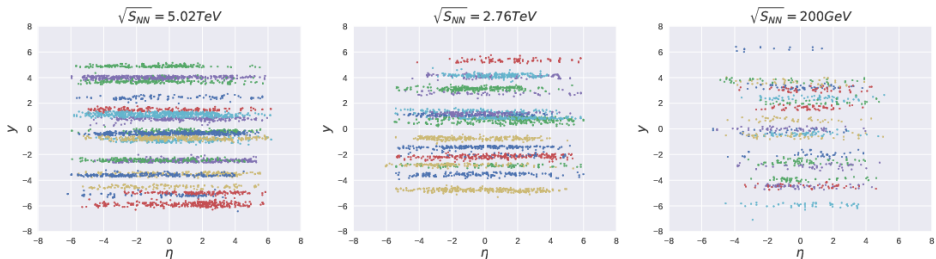
Collimated even if separated by a mile!
Something had to create the wave!

Realizations



Glasma tubes:

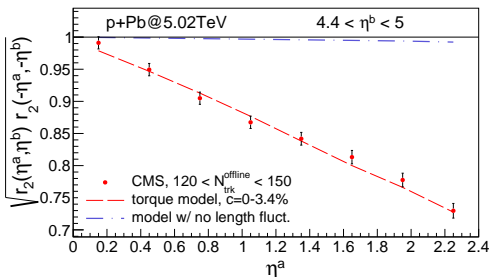
AMPT (HIJING, Lund model) [Wu et al. 2018]:



string breaking crucial \rightarrow

Torque (decorrelation) in p-Pb

- String breaking essential to describe torque in p-Pb



- cf. Huang on Monday, Bożek and Qin on Tuesday

Not covered at IS19: longitudinal fluctuations

a_{nm} coefficients

[Bzdak, Teaney, 2012, Jia, Radhakrishnan, Zhou, 2016, Monnai, Schenke, PLB 752 (2016) 317, PB, WB, Olszewski, Phys.Rev. C92 (2015) 054913, [ATLAS](#)]

p-A, how small?

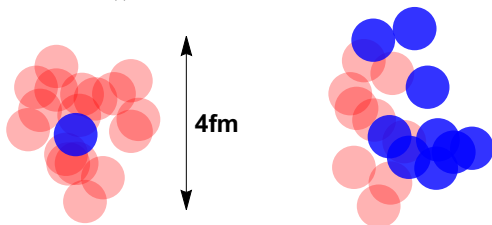
Initial fireball in p -Pb vs Pb-Pb

Sample transverse-plane configuration of centers of the participant nucleons in a p +Pb collision from GLISSANDO

5% of collisions have more than 18 participants, rms ~ 1.5 fm – quite large!

p -Pb@5.02 TeV, $N_W=18$

Pb-Pb@2.76 TeV, $N_W=18$



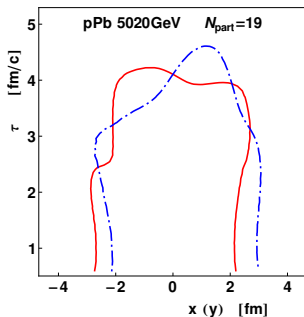
Size reflects the NN inelasticity profile

Most central values of N_w in p -Pb would fall into the 60-70% or 70-80% centrality class in Pb+Pb

Pb+Pb: $c=60-70\% \equiv 22 \leq N_w \leq 40$, $c=70-80\% \equiv 11 \leq N_w \leq 21$

Hydro evolution of the p -Pb fireball

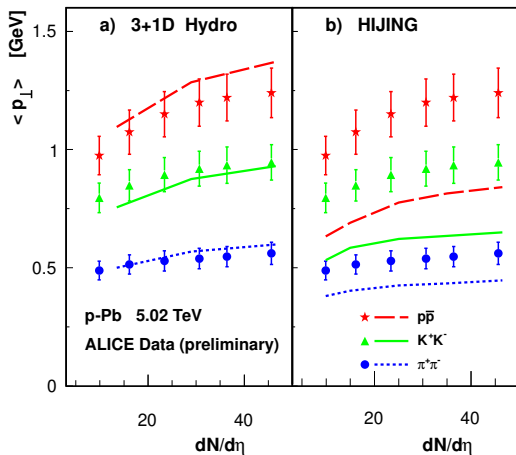
Not so small!



isotherms at freeze-out $T_f = 150$ MeV
(for two sections in the transverse plane)

- evolution lasts about 4 fm/c – shorter but more rapid than in Pb+Pb
- strong gradients \rightarrow essential role of viscosity

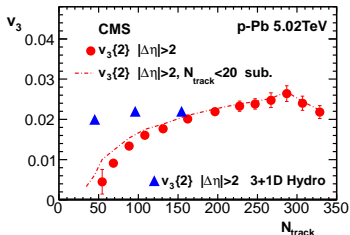
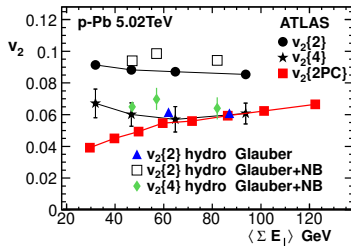
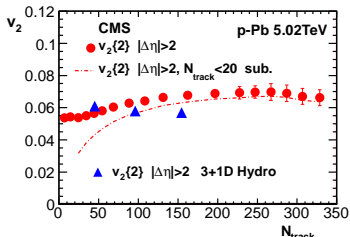
Mass hierarchy in p -A



[PB, WB, Torrieri, PRL 111 (2013) 172303]

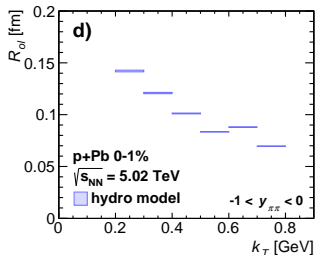
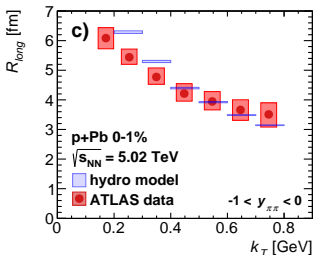
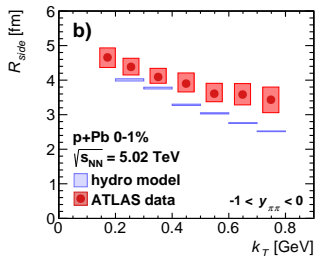
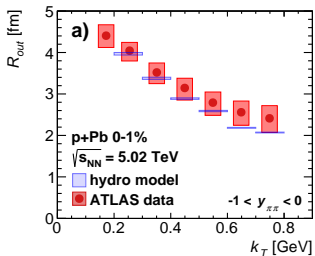
Harmonic flow in p -A

- see experimental talks!



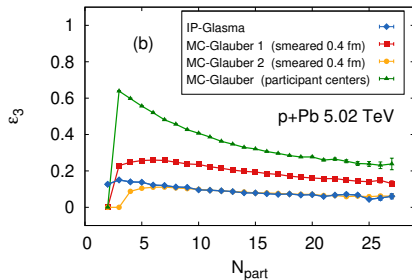
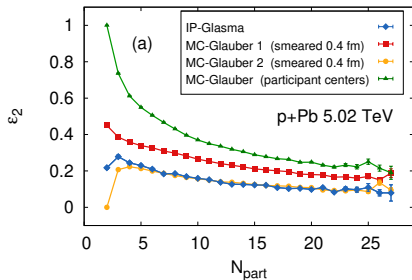
[PB, WB, PRC 88 (2013) 014903]

Interferometry



[PB, Bysiak, 2017]

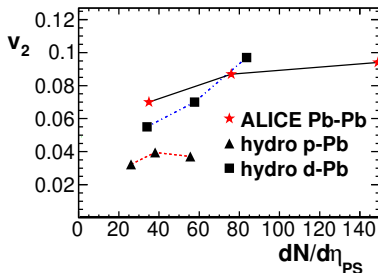
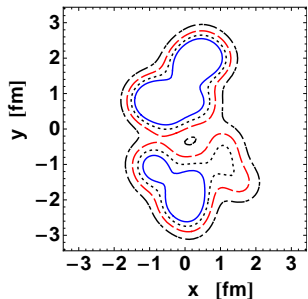
Can we distinguish approaches by the initial condition?



[Bzdak, Schenke, Tribedy, Venugopalan, Phys.Rev. C87 (2013) 064906]

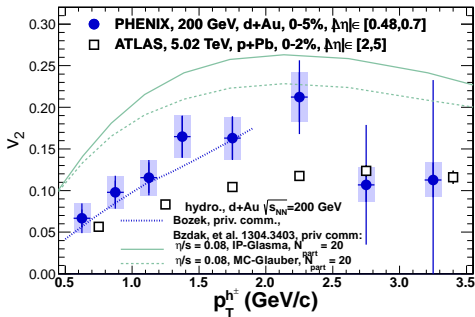
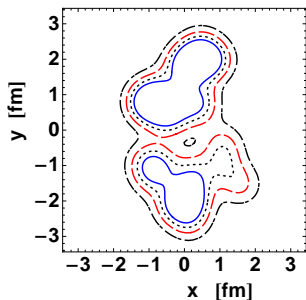
d -A, ${}^3\text{He}$ -Au

[pioneered by Bożek 2012]

intrinsic dumbbell shape with large deformation: rms $\simeq 2$ fminitial entropy density in a d-Pb collision with $N_{\text{part}} = 24$ 

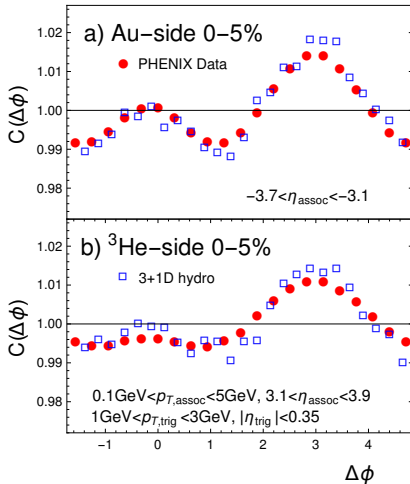
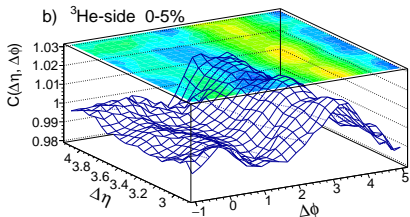
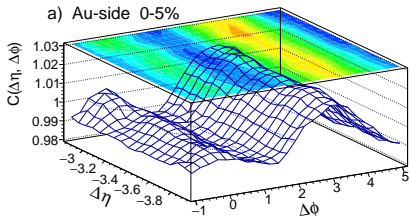
Resulting large elliptic flow confirmed with the later RHIC analysis
(geometry + fluctuations)

[pioneered by Bożek 2012]

intrinsic dumbbell shape with large deformation: rms $\simeq 2$ fminitial entropy density in a d-Pb collision with $N_{\text{part}} = 24$ 

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(geometry + fluctuations)

Ridge in $^3\text{He-Au}$ at RHIC

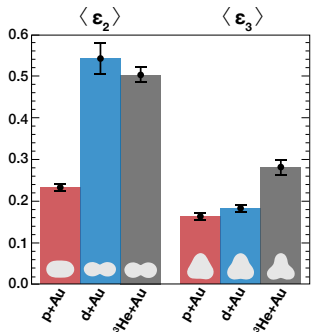


(seen on both pseudorapidity sides)

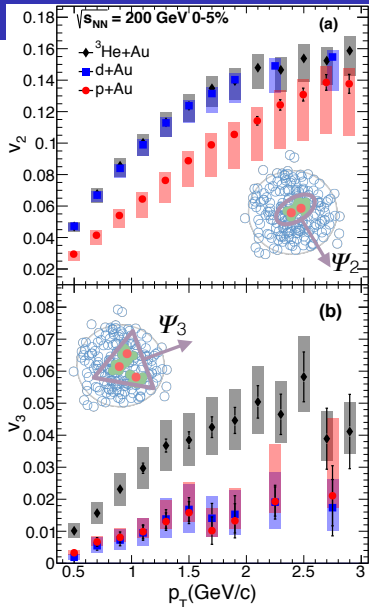
[PB, WB 2015]

Flow hierarchy in small systems

[PHENIX, 2018]

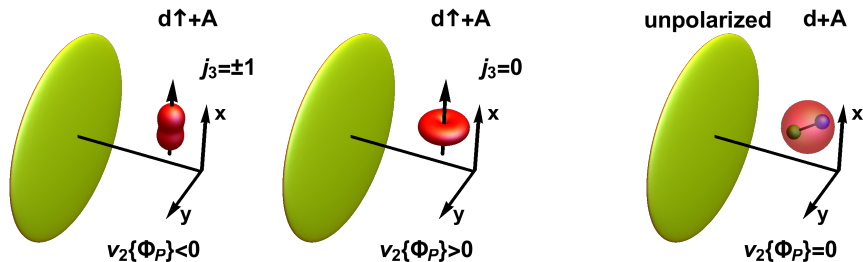


- see talks by Mace, Zajc, poster by Nagle



Controlling the geometry: A – polarized d collisions

Polarized d+A collisions

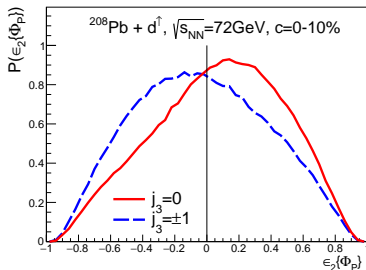
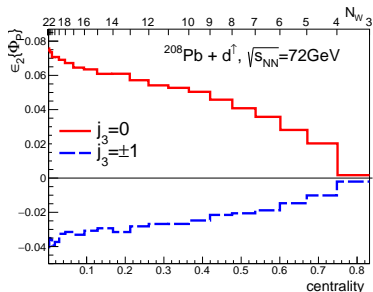


Admixture of the D -wave allows us to control the geometry! Small but measurable effect

[PB, WB, PRL 121 (2018) 202301]

Ellipticity of the fireball relative to polarization axis

GLISSANDO:

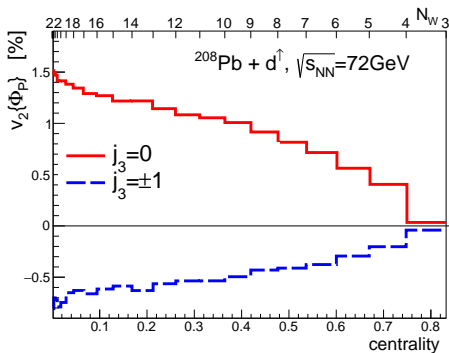


Predictions

one-body (!)

$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos[2(\phi - \Phi_P)]$$

$$v_2 \simeq k\epsilon_2, \quad k \sim 0.2$$



For $j = 1$ nuclei the *tensor polarization* is

$$P_{zz} = n(1) + n(-1) - 2n(0)$$

$$v_2\{\Phi_P\} \simeq k\epsilon_2^{j_3=\pm 1}\{\Phi_P\}P_{zz}, \quad -1.5 \leq P_{zz} \leq 0.7$$

$$-0.5\% \lesssim v_2\{\Phi_P\} \lesssim 1\%$$

One-particle distribution – can be measured precisely! Random fluctuations cancel
Single spin asymmetry $\sim \sin(\phi - \Phi_P)$ innocuous

NA61@SPS, AFTER@LHC – difficulty in injecting a polarized gas target into the Pb beam

- see talks by Schmidt, Di Nezza

2.76A TeV Pb beam on a fixed target $\rightarrow \sqrt{s_{NN}} = 72$ GeV, at LHCb
 $-2.3 < \eta_{CM} < 0.7$

[C. Barschel, Ph.D. thesis, (2014)

R. Aaij et al. (LHCb), JINST 9, P12005 (2014), arXiv:1410.0149]

Estimate of $\epsilon_2\{\Phi_P\}$ from Q_2

Quadrupole moment:

$$Q_2 = \left\langle r^2 \sqrt{\frac{16\pi}{5}} Y_{20}(\Omega) \right\rangle = \langle 3z^2 - r^2 \rangle$$

$$\epsilon_2\{\Phi_P\} \sim -\frac{3Q_2}{4Z\langle r^2 \rangle}$$

(with the approx. that neutrons follow protons)

Wigner-Eckart theorem (\hat{Q}_2 is a rank-2 tensor):

$$\langle jj_3 | \hat{Q}_{20} | jj_3 \rangle = \langle jj_3 20 | jj_3 \rangle \langle j || \hat{Q}_2 || j \rangle$$

The lowest possible j is 1 (no effect for ^3He or tritium, where $j = \frac{1}{2}$)

Estimates based on nuclear data

	j	j_3	$\langle r^2 \rangle_{\text{ch}}^{1/2}$ [fm]	Q_2 [fm ²]	$-\frac{3Q_2}{4Z\langle r^2 \rangle}$ [%]
d	1	± 1	2.1421(88)	0.2860(15)	-5.6
		0		$\times(-2)$	$\times(-2)$
⁷ Li	$\frac{3}{2}$	$\pm \frac{3}{2}$	2.444(42)	-4.03(4)	19
		$\pm \frac{1}{2}$		$\times(-1)$	$\times(-1)$
⁹ Be	$\frac{3}{2}$	$\pm \frac{3}{2}$	2.519(12)	5.29(4)	-17
		$\pm \frac{1}{2}$		$\times(-1)$	$\times(-1)$
¹⁰ B	± 3	± 3	2.428(50)	8.47(6)	-25
		± 2		$\times 0$	0
		± 1		$\times(-3/5)$	$\times(-3/5)$
		0		$\times(-4/5)$	$\times(-4/5)$

$$v_2\{\Phi_P\} \simeq -k \frac{3Q_2}{4Z(\langle r^2 \rangle + \frac{3}{2}\langle b^2 \rangle)} \frac{3j_3^2 - j(j+1)}{j(2j-1)} P$$

Light clustered nuclei

^{12}C -A – role of α clusters

“Futurology” from [WB, Ruiz Arriola, PRL 112 (2014) 112501]

Nuclear structure from ultra-relativistic collisions!

Probe to what degree ^{12}C is made of three α 's

Specific features of the ^{12}C collisions with a “wall” of Pb or Au:

The cluster plane parallel or perpendicular to the transverse plane:



higher multiplicity
higher triangularity
lower ellipticity



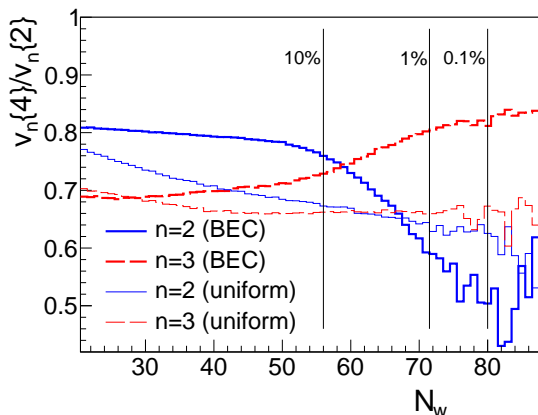
lower multiplicity
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[PB, WB, Ruiz Arriola, Rybczyński. PRC90 (2014) no.6, 064902]

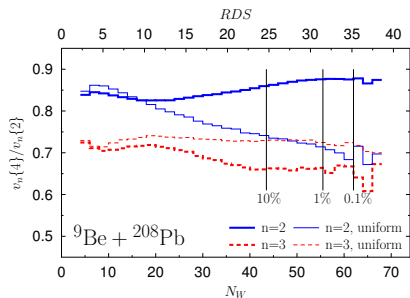
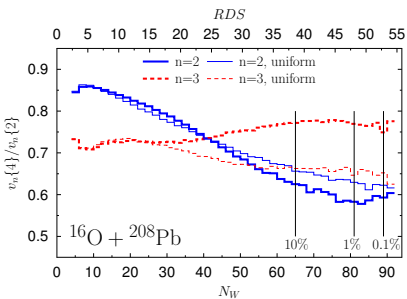
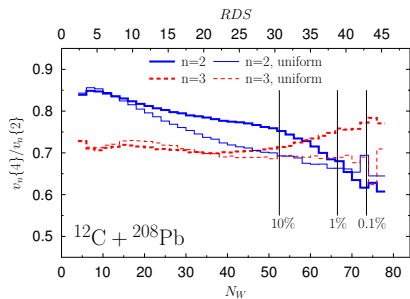
→ effects of geometric arrangement for most central

$v_n\{4\}/v_n\{2\}$ a good response-invariant probe (recall $v_n \simeq \kappa \epsilon_n$, $n = 2, 3$)

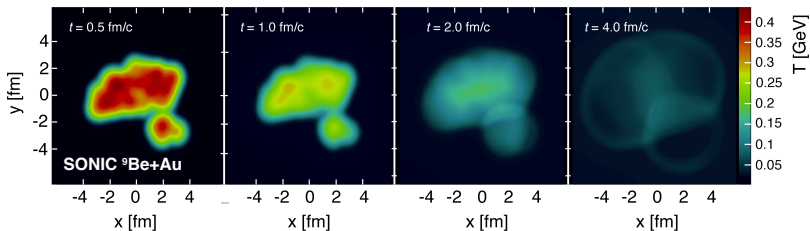
[see also Giacalone, Noronha-Hostler, Ollitrault, PRC95 (2017) 054910]



light - ^{208}Pb , $\sqrt{s_{NN}} = 17$ GeV (SPS)



Idea picked up in [Lim, Carlson, Loizides, Lonardonni, Lynn, Nagle, Orjuela Koop, Ouellette, PRC 99 (2019) 044904] [with exp. prospects](#)



two α clusters and the neutron

Summary

- Shape-flow transmutation in small systems
- Much to see in longitudinal fluctuations
- Polarized deuteron - controlled geometry
- Clustered small nuclei - insight into nuclear structure from harmonic flow

Observable or effect	PbPb	pPb (at high mult.)	pp (at high mult.)
Low p_T spectra (“radial flow”)	yes	yes	yes
Intermed. p_T (“recombination”)	yes	yes	yes
Particle ratios Statistical model	GC level $\gamma_s^{GC} = 1, 10\text{--}30\%$	GC level except Ω $\gamma_s^{GC} \approx 1, 20\text{--}40\%$	GC level except Ω $\gamma_s^C < 1, 20\text{--}40\% ^2$
HBT radii ($R(k_T), R(\sqrt[3]{N_{ch}})$)	$R_{out}/R_{side} \approx 1^3$	$R_{out}/R_{side} \lesssim 1$	$R_{out}/R_{side} \lesssim 1$
Azimuthal anisotropy (v_n) (from two part. correlations)	$v_1 - v_7$	$v_1 - v_5$	v_2, v_3
Characteristic mass dependence	v_2, v_3^4	v_2, v_3	v_2
Directed flow (from spectators)	yes	no	no
Higher order cumulants (mainly $v_2\{n\}, n \geq 4$)	“ $4 \approx 6 \approx 8 \approx \text{LYZ}$ ” +higher harmonics	“ $4 \approx 6 \approx 8 \approx \text{LYZ}$ ” +higher harmonics	“ $4 \approx 6$ ” ⁵
Weak η dependence	yes	yes	not measured
Factorization breaking	yes ($n = 2, 3$)	yes ($n = 2, 3$)	not measured
Event-by-event v_n distributions	$n = 2 - 4$	not measured	not measured
Event plane and v_n correlations	yes	not measured	not measured
Direct photons at low p_T	yes	not measured	not measured ⁶
Jet quenching	yes	not observed ⁷	not measured ⁸
Heavy flavor anisotropy	yes	hint ⁹	not measured