

1) CONSIDER THE WAVE FUNCTION

$$\psi(x) = N \sqrt{1-x^2} e^{i(1-x^2)}$$

a) Determine N

b) Determine the probability to find the particle between $-\frac{1}{2} < x < \frac{1}{2}$ by a measurement of the position.

c) Determine $\langle x \rangle$, $\langle x^2 \rangle$, Δx

d) Determine $\langle p \rangle$, $\langle p^2 \rangle$, Δp . Check if $\Delta x \Delta p$ fulfills Heisenberg uncertainty relation.

2) CONSIDER AN e^- IN A H-atom WITH THE FOLLOWING WAVE FUNCTION

$$|\psi\rangle = \alpha |1, 0, 0\rangle + \beta |2, 0, 0\rangle + \delta (|2, 1, -1\rangle + |2, 1, 1\rangle + |2, 1, 0\rangle)$$

WHERE THE USUAL $|l, m\rangle$ NOTATION IS USED

a) which conditions do α, β, δ fulfill?

b) which conditions should α, β, δ fulfill in order that $|\psi\rangle$ is an eigenvector of the Hamiltonian operator?

c) which conditions should α, β, δ fulfill in order that $|\psi\rangle$ is an eigenvector of L^2 ?

d) which conditions should α, β, δ fulfill in order that $|\psi\rangle$ is an eigenvector of L_z ?

Determine for b, c, d the corresponding eigenvalues

e) Determine the constants α, β, δ under the assumptions that (i) they are real (ii) $|\psi\rangle$ is an eigenvector of H (iii) the prob. to find $2\hbar^2$ by a measurement of L^2 is equal to 50%.

3) DETERMINE THE EIGENVALUES OF THE POTENTIAL

$$V(x) = \begin{cases} \frac{1}{2} m \omega^2 x^2 & x > 0 \\ \infty & x \leq 0 \end{cases}$$

NO CALCULATIONS ARE NEEDED
(USE THE RESULTS OF THE STANDARD H.O. AND
"EXTRAPOLATE").